

Statistical Models of Average Path Loss

Exercise 1: What is the free-space path loss, in dB, at 10 m for $f = 1500$ MHz? What is the value of $PL(1 \text{ km})$?

from Friis equation
(using $G_T = G_R = 1$)

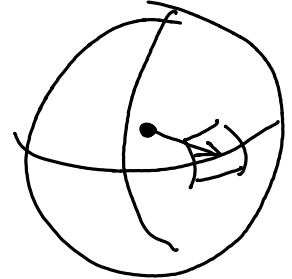
$$P_L = \frac{P_R}{P_T} = \left(\frac{\lambda}{4\pi d} \right)^2$$

$$\lambda = \frac{c}{f} = \frac{3 \times 10^8}{1.5 \times 10^9} = 0.2 \text{ m}$$

$$d = 10 \text{ m}$$

$$P_L = \left(\frac{0.2}{4\pi \cdot 10} \right)^2 = 2.5 \times 10^{-6}$$

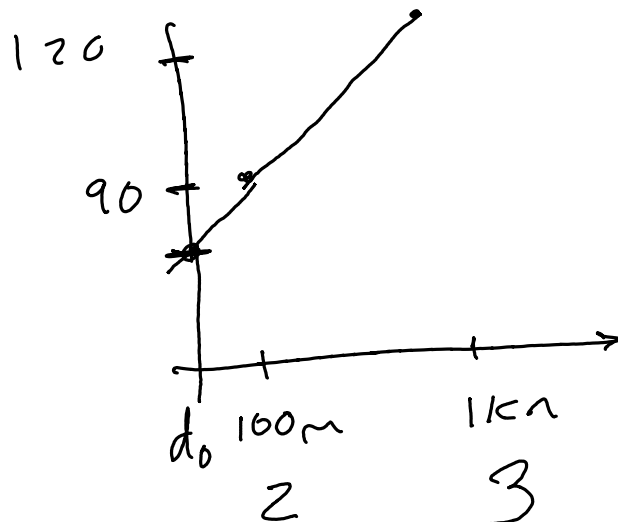
$$P_L \text{ (dB)} = -56 \text{ dB}$$



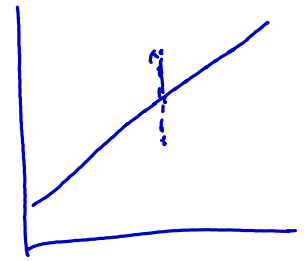
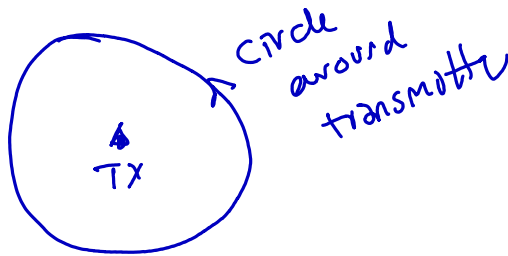
$$10 \times \log \left(\frac{0.2^2}{4 \times \pi \times 10^2} \right)^2 = -55.96359737$$

Exercise 2: If the path loss is 90 dB at 100 m and 120 dB at $d = 1 \text{ km}$, what are n and $PL(d_0 = 1 \text{ m})$?

$$PL(d)_{\text{dB}} = \underline{PL(d_0)} + 10n \log \left(\frac{d}{d_0} \right)$$



Exercise 3: What path would you have to travel if you wanted to measure the average path loss at a given distance from a particular transmitter?



Exercise 4: Compute the median path loss predicted by the Okumura-Hata model at $f = 900\text{MHz}$, base station and mobile antenna heights of 30m and 1m respectively, and a distance of 2km.

$$L_b = 69.55 + 26.16 \cdot \log \frac{f}{\text{MHz}} - 13.82 \cdot \log \frac{h_{\text{Base}}}{\text{m}} - a(h_{\text{Mobile}}) + (44.9 - 6.55 \cdot \log \frac{h_{\text{Base}}}{\text{m}}) \cdot \log \frac{d}{\text{km}}$$

$$\begin{aligned} \log 900 &= 2.95 \approx 3 \\ \log 30 &= 1.47 \approx 1.5 \\ \log 2 &= 0.3 \end{aligned}$$

where:

$$a(h_{\text{Mobile}}) = (1.1 \cdot \log \frac{f}{\text{MHz}} - 0.7) \frac{h_{\text{Mobile}}}{\text{m}} - (1.56 \cdot \log \frac{f}{\text{MHz}} - 0.8) \quad a = 2.4 \approx 3.7 \sim -1 \text{ dB}$$

The model is restricted to:

f :	150 ... 1000 MHz
h_{Base} :	30 ... 200 m
h_{Mobile} :	1 ... 10 m
d :	1 ... 20 km

$$L_b \approx 139 \text{ dB} ??$$

1) "log" means "log₁₀"

Exercise 5: A cellular system is designed so that users on the cell edge have an average SNR of 16 dB. The system requires that users have a minimum SNR of 8dB to place a call. The standard deviation of the log-normal fading is 8dB. What fraction of users at the cell edge will be able to place calls?

$$z \text{ is SNR} \quad \sigma = 8 \text{ dB}$$

find the area.

