

RF Design - Noise

Exercise 1: What are the minimum possible values of T_e and F ?

if amplifier adds no noise $kT_eB = 0$

minimum $T_e = 0$

$$\text{Then } F = \frac{T + T_e}{T} = 1$$

if $T_e > 0$ $F > 1$ (0 dB)

Exercise 2: The datasheet for a low-noise amplifier (LNA) specifies a noise figure of 2 dB. What is the noise temperature T_e ?

$$2 \text{ dB} = 10^{\frac{2}{10}} = 1.6$$

$$F = \frac{T_0 + T_e}{T_0} = \frac{290 + T_e}{290} = 1.6$$

$$T_e = (1.6 \cdot 290) - 290 \\ \approx \underline{\underline{169.6 \text{ K}}}$$

Exercise 3: An LNA with a noise figure of 0.3 dB receives a signal with an SNR of 6 dB. What is the output SNR?

$$0.3 \text{ dB} = 10^{\frac{0.3}{10}}$$

$$6 \text{ dB} = 4$$

$$F = \frac{S_i/N_i}{S_o/N_o} = 1.07 = \frac{4}{S_o/N_o}$$

$$S_o/N_o = \frac{4}{1.07} = 3.73 = 5.7 \text{ dB}$$

Exercise 4: A What is the system noise figure of a receiver that consists of a 10 dB amplifier with 3 dB noise figure followed by a mixer with a 6 dB loss and an IF amplifier with a 20dB gain and a noise figure of 10 dB?

$$G_1 = 10 \text{ dB} = 10$$

$$F_1 = 3 \text{ dB} = 2$$

$$G_2 = -6 = \frac{1}{4}$$

$$F_2 = 6 = 4$$

$$G_3 = 20 = 100$$

$$F_3 = 10 = 10$$

$$F = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 G_2}$$

$$= 2 + \frac{4 - 1}{10} + \frac{10 - 1}{10 \cdot \frac{1}{4}}$$

$$= 2 + 0.3 + 3.6$$

$$= 5.9 \approx 8 \text{ dB}$$