Tackling the Load Uncertainty Challenges for Energy Consumption Scheduling in Smart Grid

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Abstract-In this paper, we propose a novel optimizationbased real-time residential load management algorithm that takes into account load uncertainty in order to minimize the energy payment for each user. Unlike most existing demand side management algorithms that assume perfect knowledge of users' energy needs, our design only requires knowing some statistical estimates of the future load demand. Moreover, we consider realtime pricing combined with inclining block rate tariffs. In our problem formulation, we take into account different types of constraints on the operation of different appliances such as mustrun appliances, controllable appliances that are interruptible, and controllable appliances that are not interruptible. Our design is multi-stage. As the demand information of the appliances is gradually revealed over time, the operation schedule of controllable appliances is updated accordingly. Simulation results confirm that the proposed energy consumption scheduling algorithm can benefit both users, by reducing their energy expenses, and utility companies, by improving the peak-to-average ratio of the aggregate load demand.

Keywords: Demand side management, energy consumption control, cost minimization, load uncertainties, smart power grid.

I. LIST OF VARIABLES USED IN THIS PAPER

- Set of appliances \mathcal{A}
- T Number of time slots
- Nominal power of appliance a
- $\gamma_a \\ E_a$ Total required energy of appliance a
- β_a Operating deadline of appliance a
- State of power consumption of appliance a at time slot t
- $\begin{array}{c} x_t^a \\ E_t^a \\ E_t^a \end{array}$ Remaining required energy of appliance a at time slot t
- l_t Total household power consumption at time slot t
- $\lambda_t(\cdot)$ Price function at time slot t
- Price parameter at time slot t m_t
- Price parameter at time slot t n_t
- b_t Price parameter at time slot t
- Set of must-run appliances that are awake at time slot t $\mathcal{M}_{k,t}$ and remain awake at time slot k > t
- $\hat{\mathcal{M}}_{k,t}$ Set of must-run appliances that are asleep at time slot tand will be awake at time slot $k \ge t$
- $\tilde{\mathcal{M}}_k$ Set of all must-run appliances that are awake at time slot $k (\mathcal{M}_{k,t} \cup \mathcal{M}_{k,t})$
- Set of controllable appliances that are awake at time slot $\mathcal{C}_{k,t}$ t and remain awake at time slot k > t
- $\hat{\mathcal{C}}_{k,t}$ Set of controllable appliances that are asleep at time slot t and will be awake at time slot $k \ge t$

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- $\tilde{\mathcal{C}}_k$ Set of all controllable appliances that are awake at time slot $k (\mathcal{C}_{k,t} \cup \hat{\mathcal{C}}_{k,t})$
- $\mathcal{N}_{k,t}$ Set of non-interruptible appliances of $C_{k,t}$
- $\hat{\mathcal{N}}_{k,t}$ Set of non-interruptible appliances of $\hat{C}_{k,t}$
- Set of all non-interruptible appliances that are awake at $\tilde{\mathcal{N}}_k$ time slot $k (\mathcal{N}_{k,t} \cup \hat{\mathcal{N}}_{k,t})$
- \mathcal{S}_t Set of all appliances that are sleeping at time slot t
- y_k^a Auxiliary variable for each non-interruptible appliance a at each time slot \boldsymbol{k}
- MAuxiliary large number used in the problem formulation
- Auxiliary variable for each time slot k ν_k
- p_t^a Probability with which appliance *a* becomes *awake* at time slot t
- Probability that appliance a does not become awake at any q_a time slot
- Probability that appliance a becomes awake at time slot $p_{\tau,t}^a$ $\tau > t$ given that it has not become awake until time slot t
- Probability that must-run appliance a which is sleeping at $\delta^a_{\tau,t}$ time slot t will be active in time slot $\tau > t$
- T_a Number of time slots required to finish the operation of appliance a

II. INTRODUCTION

Demand side management (DSM) programs are employed to better utilize the available power generation capacity and to circumvent installing new generation and transmission infrastructures [1]. DSM programs encourage users to shift their usage of high-power appliances to off-peak hours by providing economic incentives to consumers. Among different techniques considered for DSM (e.g., voluntary load management [2]-[7], direct load control [8]-[10]), smart pricing is known as an effective means to encourage users to consume wisely and more efficiently. By reflecting the hourly changes in the wholesale electricity price to the demand side, users pay what the electricity is worth at different times of day and are consequently more willing to reduce their load at peak hours.

In time differentiating pricing tariffs, the intended operation period is divided into several time slots, and the price of electricity varies across different time slots. For example, the prices may correspond to off-peak, mid-peak, and onpeak hours. The prices are usually higher in the afternoon on hot days in the summer and cold days in the winter [11]. Several time differentiating pricing methods have already been proposed in the literature. Examples include real-time pricing (RTP), time-of-use (TOU) pricing, and day-ahead pricing (DAP) [12]-[16]. These methods mainly differ in how frequently the utility company changes the pricing tariffs, which may vary from once or twice a year in TOU pricing to hourly changes in RTP. The level of success of different pricing methods depends on various factors such as the amount of information provided to each user, the effectiveness of the mapping of the hourly wholesale prices to the retail prices, and the ability of users to respond to price signals [17].

In general, it is difficult for consumers to follow the realtime prices and respond to their variations accordingly. This aspect and some other disadvantages of manual load control are discussed in [18]. An alternative approach is to equip users with automated control units that respond to real-time price signals to improve the level of *rationality* of users. Different approaches of the users in responding to price values are studied in [19], [20]. The necessity of more advanced methods to avoid efficiency loss in the system due to enhanced rationality levels of the users has been discussed in [19]. The effect of *load synchronization*, i.e., the concentration of a large portion of energy consumption in low-price hours, has been studied in [18]. It is shown that load synchronization can be prevented by using pricing tariffs with inclining block rates (IBR). For the IBR tariffs, the marginal price increases with the total consumed power [21]. That is, beyond a predetermined power consumption threshold, electricity is offered at higher rates. This provides incentives for the users to *distribute* their load across different times of the day. Southern California Edison and Pacific Gas & Electric in United States, and British Columbia Hydro in Canada currently use IBR with various two-level conservation rate structures [22], [23].

Despite its importance, the effect of load uncertainties on DSM has not been well-studied in the smart grid literature [6], [11], [19], [20], [24]–[29]. In this paper, we focus on developing a novel automated optimization-based residential load scheduling algorithm in a retail electricity market with load uncertainties. We aim to minimize each user's electricity payment by optimally scheduling the operation of its appliances in real-time, subject to the operational constraints defined by the users. As in [18], we adopt RTP *combined* with IBR to better reflect the fluctuation of the wholesale electricity prices and to avoid *load synchronization*.

Our design can be partly compared with [27]. The problem tackled in this paper is different from that in [27] in two aspects. First, the work in [27] addresses uncertainty in *price values* while we tackle uncertainty in load and users' energy consumption needs. Second, the key assumption in [27] is that the price values are *independent* from the load level in each time slot. Here, we relax this assumption. Our work is also different from the *heuristic* home automation schemes in [30], [31], as we use an optimization-based approach with elaborate mathematical modeling and take into account estimates of the future load to make better decisions. The contributions of this paper can be summarized as follows:

• We propose a real-time residential load management algorithm with *load uncertainty* for DSM purposes. Our algorithm is based on solving an optimization problem that aims to minimize the electricity payment of residential users. Each appliance sends an *admission request* to the *energy consumption control* unit to start operation. The operation of each appliance is subject to acceptance of its request. By running a centralized algorithm, the control unit determines the optimal operation schedule of each appliance in each time slot.

- We study operation constraints to model a variety of appliances including *must-run* appliances, and *interruptible* and *non-interruptible* controllable appliances. The last item refers to those appliances whose operation can be postponed, but once they start operation, they should stay on until they finish their task.
- Simulation results show that our proposed scheduling algorithm with load uncertainty reduces the energy payment of users compared to the case where no scheduling algorithm is adopted. Our proposed scheme also improves the overall power system performance by reducing the peak-to-average ratio (PAR) in aggregate load demand.

The rest of this paper is organized as follows. The system model is introduced in Section III. The problem formulation and algorithm description are presented in Section IV. Simulation results are provided in Section V. The paper is concluded in Section VI.

III. SYSTEM MODEL

In this section, we present a mathematical model for realtime residential load scheduling when combined RTP and IBR tariffs are implemented. We assume that price values are informed by the retailer to end users through a digital communication infrastructure. Furthermore, we assume that each user is equipped with a smart meter, which has an *energy consumption control* (ECC) unit capable of scheduling and adjusting the household energy consumption.

Consider a residential unit that participates in a DSM program. Let \mathcal{A} denote the set of all appliances in this unit. Each appliance $a \in \mathcal{A}$ can work either as *must-run* or controllable. Must-run appliances need to start working immediately. For example, we can classify TV and personal computer (PC) as must-run appliances. Clearly, the user should have the freedom to turn on or turn off the TV whenever he wants without the interference of the ECC. In contrast, the operation of controllable appliances can be *delayed* or *interrupted* if necessary. Each controllable appliance can be either interruptible or non-interruptible. For a controllable appliance a, if it is non-interruptible, then the ECC may only delay its operation. However, for interruptible appliances, it is not only possible to postpone the operation but also to interrupt the operation when needed and then restore the operation later on. Plug-in electric vehicle (PEV) and washing machine are examples of interruptible and non-interruptible controllable appliances, respectively. We assume that based on the demand requirements of the user, each appliance can be set as mustrun or controllable. This setting is decided by the user and can vary from time to time. That is, depending on the preferences of the user, an appliance can be set as a must-run appliance in one day and as a controllable appliance in another day.

We divide the intended operation cycle into T time slots. Each time slot begins with an *admission control* phase. In this phase, to start the operation of an appliance, an *admission request* is sent to the ECC unit. Once an admission request is submitted, the state of the appliance changes from *sleep* to *awake*. The appliance remains awake until its operation is *finished*. However, the *operation* of an awake appliance is

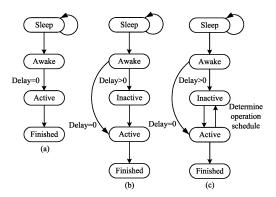


Fig. 1. Different operating states of (a) must-run, (b) non-interruptible controllable, and (c) interruptible controllable appliances.

subject to acceptance of its admission request and specification of its operation schedule by the ECC unit. The decisions regarding the admission of the requests and the adjustment of the operation of different awake appliances are updated periodically in each admission control phase.

An awake appliance *a* can be either *inactive* (with zero power consumption) or *active* (operating at nominal power γ_a). We note that the power consumption of each appliance could be different at different cycles of its operation due to the changes in the amount of current being absorbed. However, considering the exact load profile of each appliance adds to the complexity of the model and makes real-time implementation difficult. To tackle this implementation difficulty, similar to [24], [25], and [27], we consider an average power consumption γ_a for each appliance. Different operating states of mustrum and controllable appliances are shown in Fig. 1.

We note that the operation of different appliances is influenced by the preferences of the user. Different parameters of our model may be considered to capture different types of preferences. For example, our model takes into account the time and the frequency at which each appliance sends admission requests to the ECC unit. Furthermore, we assume that the mode of operation of each appliance, i.e., whether it is must-run or controllable, is *not* pre-determined. That is, based on the preference of the user, each appliance can work either as must-run or controllable. Moreover, for controllable appliances, the deadline before which the operation of the appliance has to be finished is also determined based on the preference of the user. Other aspects of user preferences, such as the desirable room temperature, can also be considered to enhance energy consumption scheduling; however, adding those aspects will also make the design more complex and less appealing for *real-time* implementation in practice.

The admission request of each appliance a specifies the total energy E_a needed to finish the operation of the appliance, the operating power γ_a , and whether the appliance is mustrun or controllable. For controllable appliances, the deadline before which the operation of the appliance has to be finished, denoted by β_a , and whether it is interruptible or not, are the additional information to be included in the admission request. For a controllable appliance a, if it is not interruptible, the ECC may only delay its operation. However, for interruptible appliances, it is not only possible to postpone the operation but also to interrupt the operation when needed. We define binary variable $x_t^a \in \{0, 1\}$ as the state of power consumption of appliance $a \in \mathcal{A}$ at time slot $t \in \{1, \ldots, T\}$. We set $x_t^a = 1$ if appliance a is admitted to operate in time slot t (i.e., *active*), otherwise, we set $x_t^a = 0$ (i.e., *inactive*). Let E_t^a denote the amount of energy required to finish the operation of appliance a while the current time slot is t. Note that given E_t^a , for each future time slot k > t > 0, we have

$$E_{k}^{a} = \left[E_{t}^{a} - \gamma_{a} \sum_{i=t}^{k-1} x_{i}^{a}\right]^{+}.$$
 (1)

For controllable appliances that are *non-interruptible*, their operation can be delayed, but once they become active, they must remain active until the end of their operation. Thus, for each non-interruptible controllable appliance a, we have

$$x_k^a = 1, \quad \forall k \in \{t, \dots, \beta_a\}, \ 0 < E_k^a < E_a.$$
 (2)

Let $l_t \triangleq \sum_{a \in \mathcal{A}} \gamma_a x_t^a$ denote the total household power consumption at time slot t. We consider a pricing function $\lambda_t(l_t)$ which represents the price of electricity in each time slot t as a function of the user's power consumption in that time slot. For combined RTP and IBR pricing tariffs, the price function $\lambda_t(l_t)$ is defined as [18]:

$$\lambda_t(l_t) = \begin{cases} m_t, & \text{if } 0 \le l_t \le b_t, \\ n_t, & \text{if } l_t > b_t, \end{cases}$$
(3)

where m_t , n_t , and b_t are pre-determined parameters. We have $m_t \leq n_t$. Recall from Section II that a combined RTP and IBR pricing model can effectively avoid load synchronization [18].

IV. PROBLEM FORMULATION AND ALGORITHM DESCRIPTION

In this section, we consider the problem of *efficient power* scheduling such that the electricity payment of each user is minimized. We assume that only some statistical demand information are known ahead of time. The exact information about the list of appliances that are awake in each time slot, whether they are must-run or controllable, and the deadline by which the operation of each appliance should be finished is revealed only gradually over time. We note that different sets of awake appliances, i.e., must-run and controllable, at future time slot k > t, can be separated into two disjoint subsets. The first subset includes those appliances that are awake at the current time slot t and remain awake at time slot k > t, i.e., the information about this subset of appliances is known at the current time slot. The second subset consists of those appliances that are asleep at the current time slot t and will be awake at time slot k > t. However, at the current time slot t, only some statistical information about this subset of appliances is available. An update is received by the ECC unit at the beginning of each time slot, and the energy consumption schedule of each controllable appliance is adapted accordingly.

A. Problem Formulation

The optimum operation schedule can be determined if the demand information of all appliances is available at the beginning of the scheduling horizon. However, we assume here that the demand information of the appliances is not known and instead only stochastic information regarding the demand is available a priori. Thus, we formulate a scheduling problem that minimizes the *expected* energy payment of the user with respect to demand uncertainties. In each time slot t, as the demand information of the appliances is updated, the operation schedule of each controllable appliance can be rescheduled. The power scheduling can be identified in real-time as the solution of the following optimization problem:

$$\begin{array}{l} \underset{\mathbf{x}_{t}^{a}, \forall a \in \tilde{\mathcal{C}}_{k}, \\ \forall k \in \{t, \dots, T\} \end{array}}{\underset{\mathbf{x}_{k}^{a} \in \{0, 1\}, \quad \forall a \in \tilde{\mathcal{C}}_{k}, k \in \{t, \dots, T\}, \end{array}}{\mathbb{E}\left\{L_{t}\lambda_{t}\left(L_{t}\right) + \sum_{k=t+1}^{T} L_{k,t}\lambda_{k}\left(L_{k,t}\right)\right\}}$$

$$(4)$$
subject to
$$x_{k}^{a} \in \{0, 1\}, \quad \forall a \in \tilde{\mathcal{C}}_{k}, k \in \{t, \dots, T\},$$

$$\gamma_{a} \sum_{k=1}^{\beta_{a}} x_{k}^{a} = E_{t}^{a}, \quad \forall a \in \tilde{\mathcal{C}}_{k},$$

$$x_k^{a=t} = 1, \ \forall a \in \tilde{\mathcal{N}}_k, \ k \in \{t, \dots, \beta_a\}, \\ 0 < E_k^a < E_a$$

where $\mathbb{E}\{\cdot\}$ denotes the expectation,

$$L_t = \sum_{a \in \tilde{\mathcal{M}}_t} \gamma_a + \sum_{a \in \tilde{\mathcal{C}}_t} \gamma_a x_t^a,$$
(5)

$$L_{k,t} = \sum_{a \in \mathcal{M}_{k,t}} \gamma_a + \sum_{a \in \hat{\mathcal{M}}_{k,t}} \gamma_a + \sum_{a \in \mathcal{C}_{k,t}} \gamma_a x_k^a + \sum_{a \in \hat{\mathcal{C}}_{k,t}} \gamma_a x_k^a,$$
(6)

 $\mathbf{x}_t^a \triangleq (x_t^a, \dots, x_T^a), E_k^a$ is as in (1), and the definitions of the different sets of appliances $\mathcal{M}_{k,t}$, $\hat{\mathcal{M}}_{k,t}$, $\tilde{\mathcal{M}}_t$, $\mathcal{C}_{k,t}$, $\hat{\mathcal{C}}_{k,t}$, $\tilde{\mathcal{C}}_k$, and $\tilde{\mathcal{N}}_k$ are presented in Section I. We note that E_t^a is known at time slot t, must-run appliances are *active* as long as they are *awake*, $\mathcal{C}_{k,t} = \mathcal{C}_{t,t}$ for all $k \ge t$, and as the demand information is known up to time slot t, $\hat{\mathcal{M}}_{t,t} = \hat{\mathcal{C}}_{t,t} = \emptyset$. The first term in the objective function in (4) is the payment of the user in the current time slot t for the known load L_t , while the second term is the expected cost of energy in the upcoming time slots. Each appliance can be either on or off. This is indicated by the first constraint. The second constraint implies that the operation of each appliance should be finished by its deadline. The last constraint guarantees that the operation of non-interruptible appliances will continue after they become active until they finish their job.

In our stochastic model, it is possible to devise different objectives and different strategies to schedule the operation of different appliances. The performances of different scheduling strategies are different. However, their different performances may be compared based on their average performance and their worst case performance for different demand requirements of the user. Problem (4) in its current form is difficult to solve as it requires the computation of the expected schedule for currently sleeping appliances¹. To tackle this problem, we minimize an *upper bound* of the objective function. We assume

¹One option to solve problem (4) is to formulate it as a *dynamic programming problem*. Considering the amount of information required to describe the state of each appliance, i.e., whether the appliance is awake or not, the remaining energy requirements, and the number of time slots remaining to reach the deadline, we may be faced with a huge state space of outcomes. Dynamic programming may suffer from the *curse of dimensionality* [32].

all appliances that become awake in future time slots are mustrun appliances. In this case, the *risk of loss* for the user is minimized. That is, from the the user's electricity payment point of view, the worst performance of the ECC unit for different scheduling strategies is minimized.

 $\begin{array}{ll} \underset{\mathbf{x}_{t}^{a}, \forall \ a \in \tilde{\mathcal{C}}_{t}}{\text{minimize}} & L_{t}\lambda_{t}\left(L_{t}\right) + \sum_{k=t+1}^{T} \mathbb{E}\left\{\bar{L}_{k,t}\lambda_{k}\left(\bar{L}_{k,t}\right)\right\} & (7) \\ \text{subject to} & x_{k}^{a} \in \{0,1\}, \quad \forall \ a \in \tilde{\mathcal{C}}_{t}, \ k \in \{t,\ldots,T\}, \\ & \gamma_{a}\sum_{k=t}^{\beta_{a}} x_{k}^{a} = E_{t}^{a}, \quad \forall \ a \in \tilde{\mathcal{C}}_{t}, \\ & x_{k}^{a} = 1, \ \forall \ a \in \tilde{\mathcal{N}}_{t}, \ k \in \{t,\ldots,\beta_{a}\}, \\ & 0 < E_{k}^{a} < E_{a}, \end{array}$

where

$$\bar{L}_{k,t} = \sum_{a \in \mathcal{M}_{k,t}} \gamma_a + \sum_{a \in \hat{\mathcal{M}}_{k,t} \cup \hat{\mathcal{C}}_{k,t}} \gamma_a + \sum_{a \in \mathcal{C}_{k,t}} \gamma_a x_k^a \quad (8)$$

denotes the load at time slot k > t.

Problem (7) is still difficult to solve in its current form since the last constraint is conditioned on the value of E_k^a for $k \in$ $\{t+1,\ldots,\beta_a\}$. From (1), for $k \in \{t+1,\ldots,\beta_a\}$, E_k^a depends on variable x_i^a for $i \in \{t,\ldots,k-1\}$, which is unknown and should be determined. However, by introducing an auxiliary variable $y_k^a \in \{0,1\}$ for each appliance $a \in \tilde{N}_t$ and at each time slot $k \in \{t+1,\ldots,\beta_a\}$, the problem formulation in (7) can be re-written in a more tractable form. Here, the auxiliary variable y_k^a indicates whether the operation of appliance a is finished $(y_k^a = 1)$ or not $(y_k^a = 0)$ at a particular time slot $k \in \{t+1,\ldots,\beta_a\}$. Thus, we can re-write problem (7) as

$$\underset{\substack{\mathbf{x}_{t}^{a}, \forall a \in \tilde{\mathcal{C}}_{t} \\ \mathbf{y}_{t}^{a}, \forall a \in \tilde{\mathcal{N}}_{t}}{\text{minimize}} \quad L_{t}\lambda_{t}(L_{t}) + \sum_{k=t+1}^{T} \mathbb{E}\left\{\bar{L}_{k,t}\lambda_{k}(\bar{L}_{k,t})\right\}$$

$$+M\sum_{k=t}^{T}\sum_{a\in\tilde{\mathcal{C}}_{t}}y_{k}^{a}\tag{9}$$

subject to $x_k^a \in \{0, 1\}, \ \forall \ a \in \tilde{\mathcal{C}}_t, \ k \in \{t, \dots, T\},$ (10)

$$y_k^a \in \{0, 1\}, \ \forall \ a \in \tilde{\mathcal{N}}_t, \ k \in \{t, \dots, T\},$$
 (11)

$$\gamma_a \sum_{k=t}^{\beta_a} x_k^a = E_t^a, \quad \forall \, a \in \tilde{\mathcal{C}}_t, \tag{12}$$

$$y_k^a + \frac{E_t^a - \gamma_a \sum_{i=t}^{k-1} x_i^a}{E_a} \ge \epsilon,$$

$$\forall a \in \tilde{\mathcal{N}}_t, \ k \in \{t, \dots, \beta_a\}, \quad (13)$$

$$x_k^a + y_k^a + \frac{E_t^a - \gamma_a \sum_{i=t}^{k-1} x_i^a}{E_a} \ge 1,$$

$$\forall a \in \tilde{\mathcal{N}}_t, \ k \in \{t, \dots, \beta_a\}, \quad (14)$$

where $\mathbf{y}_t^a \triangleq (y_t^a, \dots, y_T^a)$, M is a constant, and $0 < \epsilon < \min\{\frac{\gamma_1}{E_1}, \dots, \frac{\gamma_{|\mathcal{A}|}}{E_{|\mathcal{A}|}}\}$ is a small constant. We can justify the

new constraints as follows. In (13), when $E_k^a = E_t^a - \gamma_a \sum_{i=t}^{k-1} x_i^a = 0$, y_k^a becomes 1. However, as long as the operation is not finished, i.e., $E_k^a > 0$, since y_k^a appears in the objective of the minimization problem, we have $y_k^a = 0$. This is true, since for any value $E_k^a > 0$, we have $\frac{E_k^a}{E_a} > \epsilon$. In (14), when $E_k^a = E_a$, we have $y_k^a = 0$, and x_k^a could be either 0 or 1, when $E_a > E_k^a > 0$, we have $y_k^a = 1$, and since x_k^a appears in the objective of the minimization problem, it has to be 0.

For the price function in (3), since $m_t \leq n_t$, for a total load l_t at time slot t, the user's payment $l_t \times \lambda_t(l_t)$ is determined as the maximum of the two intersecting lines [18]:

$$l_t \times \lambda_t(l_t) = \max\{m_t l_t, n_t l_t + (m_t - n_t)b_t\}.$$
 (15)

Thus problem (9) can be reformulated as

$$\begin{array}{l} \underset{\mathbf{x}_{t}^{a}, \forall a \in \tilde{\mathcal{C}}_{t}}{\minide \sum_{a \in \tilde{\mathcal{C}}_{t}} \gamma_{a} x_{t}^{a} + \sum_{a \in \tilde{\mathcal{M}}_{t}} \gamma_{a}} \\ n_{t} \left(\sum_{a \in \tilde{\mathcal{C}}_{t}} \gamma_{a} x_{t}^{a} + \sum_{a \in \tilde{\mathcal{M}}_{t}} \gamma_{a} \right) + (m_{t} - n_{t}) b_{t} \\ + \sum_{k=t+1}^{T} \mathbb{E} \left\{ \max \left\{ m_{k} \left(\sum_{a \in \tilde{\mathcal{C}}_{t}} \gamma_{a} x_{k}^{a} + l_{k,t} \right), \\ n_{k} \left(\sum_{a \in \tilde{\mathcal{C}}_{t}} \gamma_{a} x_{k}^{a} + l_{k,t} \right) + (m_{k} - n_{k}) b_{k} \right\} \\ + M \sum_{k=t}^{T} \sum_{a \in \tilde{\mathcal{C}}_{t}} y_{k}^{a} \end{array} \right) \tag{16}$$

subject to (10) - (14),

subject to (10) - (14),

where

$$l_{k,t} \triangleq \sum_{a \in \mathcal{M}_{k,t}} \gamma_a + \sum_{a \in \hat{\mathcal{M}}_{k,t} \cup \hat{\mathcal{C}}_{k,t}} \gamma_a.$$
(17)

Finally, by introducing another auxiliary variable, ν_k , for each time slot k, and by adopting the *certainty equivalent* approximation technique, i.e., all uncertainties are fixed at their expected value [33], we can re-write problem (16) as

$$\underset{\substack{\boldsymbol{\nu}_{t}, \mathbf{x}_{t}^{a}, \forall a \in \tilde{\mathcal{C}}_{t} \\ \mathbf{y}_{t}^{a}, \forall a \in \tilde{\mathcal{N}}_{t} }{\text{minimize}} \sum_{k=t}^{T} \nu_{k} + M \sum_{k=t}^{T} \sum_{a \in \tilde{\mathcal{C}}_{t}} y_{k}^{a}$$
(18)

$$m_t \left(\sum_{a \in \tilde{\mathcal{C}}_t} \gamma_a x_t^a + \sum_{a \in \tilde{\mathcal{M}}_t} \gamma_a \right) \le \nu_t,$$
$$n_t \left(\sum_{a \in \tilde{\mathcal{C}}_t} \gamma_a x_t^a + \sum_{a \in \tilde{\mathcal{M}}_t} \gamma_a \right) + (m_t - n_t) b_t \le \nu_t,$$

$$m_k \left(\sum_{a \in \tilde{\mathcal{C}}_t} \gamma_a x_k^a + \hat{l}_{k,t} \right) \leq \nu_k,$$

$$\forall k \in \{t+1, \dots, T\},$$

$$n_k \left(\sum_{a \in \tilde{\mathcal{C}}_t} \gamma_a x_k^a + \hat{l}_{k,t} \right) + (m_k - n_k) b_k \leq \nu_k,$$

$$\forall k \in \{t+1, \dots, T\},$$

where $\boldsymbol{\nu}_t \triangleq (\nu_t, \dots, \nu_T)$, and $\hat{l}_{k,t} \triangleq \mathbb{E}\{l_{k,t}\}$, the estimate of the power consumption of must-run appliances in an upcoming time slot $k \ge t$ will be calculated in the next sub-section. Problem (18) is a mixed-binary linear program and can be solved efficiently by using MOSEK [34]. The solution of optimization problem (18) determines the appropriate scheduling for the operation of controllable appliances. However, for interruptible appliances, only the operation schedule of the current time slot t will be executed, and the schedule of the future time slots $t + 1, \dots, T$ may change when the optimization problem is solved again in the next time slot as new information about the future load becomes available.

B. Load Estimation

In our system model, we assume that the demand information of the appliances is not known ahead of time, i.e., in (17), the set of awake appliances in the upcoming time slots k > t that are currently sleeping, $\hat{\mathcal{M}}_{k,t} \cup \hat{\mathcal{C}}_{k,t}$, is not known. Instead, only the probability with which each appliance becomes *awake* at each time slot t, p_t^a , is known before the operation cycle begins. Such information can be calculated, for example, based on the sleep and awake history of each appliance. For this purpose, we can observe a window of Nconsecutive days and mark those days in which appliance a becomes awake in a particular time slot t. The ratio of the number of marked days to the total number of observed days determines the probability with which appliance a becomes awake in time slot t, $p_t^a \triangleq \mathbb{P}(\Delta_t^a = 1)$, where Δ_t^a is a random variable that is equal to one if appliance a becomes awake in time slot t, and equal to zero otherwise. In our model, each appliance can become awake only once. If an appliance becomes awake more often, we can simply introduce virtual appliances to deal with this issue. Therefore, we have

$$\sum_{t=1}^{T} p_t^a + q_a = 1,$$
(19)

where q_a denotes the probability that appliance *a* does *not* become awake at *any* time within the DSM's operation period [1, T]. We define $p_{\tau,t}^a$ as the probability that appliance *a* becomes awake in time slot $\tau > t$ given that it has *not* become awake until time slot *t*. That is,

$$p_{\tau,t}^{a} = \mathbb{P}(\Delta_{\tau}^{a} = 1 \mid \Delta_{1}^{a} = 0, \dots, \Delta_{t}^{a} = 0).$$
 (20)

Based on Bayes rule, $p_{\tau,t}^a$ can be calculated as

$$p_{\tau,t}^{a} = \frac{\mathbb{P}(\Delta_{1}^{a} = 0, \dots, \Delta_{t}^{a} = 0 \mid \Delta_{\tau}^{a} = 1)\mathbb{P}(\Delta_{\tau}^{a} = 1)}{\mathbb{P}(\Delta_{1}^{a} = 0, \dots, \Delta_{t}^{a} = 0)}.$$
 (21)

If appliance a becomes awake at time slot $\tau > t$, it implies that it has not become awake in previous time slots. Therefore,

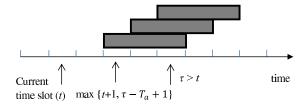


Fig. 2. Must-run appliance $a \in S_t$ with $T_a = 3$ will be active in $\tau > t$ if it starts operation within time interval $[\max\{t+1, \tau - T_a + 1\}, \tau]$.

 $\mathbb{P}(\Delta_1^a=0,\ldots,\Delta_t^a=0\mid\Delta_\tau^a=1)=1.$ On the other hand, we obtain $\mathbb{P}(\Delta_1^a=0,\ldots,\Delta_t^a=0)=\sum_{k=t+1}^T p_k^a+q_a$ based on (19). We also have $\mathbb{P}(\Delta_\tau^a=1)=p_\tau^a$. Therefore, (21) becomes

$$p_{\tau,t}^{a} = \frac{p_{\tau}^{a}}{\sum_{k=t+1}^{T} p_{k}^{a} + q_{a}}.$$
 (22)

Next, assume that all appliances that become awake in future time slots are must-run appliances, and must-run appliances start operation once they become awake, see Section IV-A. Let Λ_{τ}^{a} denote the random variable that indicates whether must-run appliance a is active $(\Lambda_{\tau}^{a} = 1)$ or not active $(\Lambda_{\tau}^{a} = 0)$ in time slot τ . Also, let $\delta_{\tau,t}^{a}$ denote the probability that a must-run appliance a which is sleeping in time slot t will be active in time slot $\tau > t$. By conditioning on the time slot in which must-run appliance a becomes awake, $\delta_{\tau,t}^{a}$ can be calculated as

$$\delta_{\tau,t}^{a} = \mathbb{P}(\Lambda_{\tau}^{a} = 1 \mid \Delta_{1}^{a} = 0, \dots, \Delta_{t}^{a} = 0)$$

= $\sum_{k=t+1}^{T} \mathbb{P}(\Lambda_{\tau}^{a} = 1 \mid \Delta_{1}^{a} = 0, \dots, \Delta_{t}^{a} = 0, \Delta_{k}^{a} = 1)p_{k,t}^{a}, \quad (23)$

where $p_{k,t}^a$ is defined in (20). As illustrated in Fig. 2, a currently sleeping appliance will be active in time slot $\tau > t$, if it starts operation within time frame $[\max\{t+1, \tau-T_a+1\}, \tau]$, where $T_a \triangleq \frac{E_a}{\gamma_a}$ is defined as the number of time slots required to finish the operation of appliance a while operating at power level γ_a . For simplicity, we assume T_a is integer. Therefore, $\mathbb{P}(\Lambda_{\tau}^a = 1 \mid \Delta_1^a = 0, \ldots, \Delta_t^a = 0, \Delta_k^a = 1) = 1$ if $k \in [\max\{t+1, \tau-T_a+1\}, \tau]$, and $\mathbb{P}(\Lambda_{\tau}^a = 1 \mid \Delta_1^a = 0, \ldots, \Delta_t^a = 0, \Delta_k^a = 1) = 0$ otherwise. Thus, we have

$$\delta^{a}_{\tau,t} = \sum_{k=\max\{t+1,\tau-T_{a}+1\}}^{\tau} p^{a}_{k,t}.$$
 (24)

Finally, by conditioning on the event of observing a currently sleeping appliance *active* in an upcoming time slot τ , while the system is at time slot t, the estimate of the power consumption required in (18) becomes:

$$\hat{l}_{\tau,t} = \mathbb{E}\left\{l_{\tau,t}\right\} = \sum_{a \in \mathcal{M}_{\tau,t}} \gamma_a + \sum_{a \in \mathcal{S}_t} \gamma_a \delta^a_{\tau,t}, \qquad (25)$$

where S_t is defined in Section I.

C. Algorithm Description

In this section, we explain the different steps of the proposed energy consumption scheduling algorithm in presence of load uncertainty (Algorithm 1) executed at each time slot t. Algorithm 1: Energy consumption scheduling algorithm in presence of load uncertainty executed at the beginning of each time slot t.

1: Receive admission requests.

- 2: Label received requests either as must-run or controllable.
- 3: Activate must-run appliances (start / continue operation).
- 4: Update $p_{\tau,t}^a$ according to (22).
- 5: Update $\delta_{\tau,t}^{a}$ according to (24).
- 6: Update $\hat{l}_{\tau,t}$ according to (25).
- 7: Update E_t^a according to (1).
- 8: Solve (18) to activate / deactivate controllable appliances.
- 9: **if** activated device is non-interruptible

10: Mark it as must-run.

Step 1: At the beginning of the admission control phase at each time slot, all received admission requests are labeled as either *must-run* or *controllable*, c.f. Lines 1 and 2.

Step 2: Activate must-run appliances $a \in M_t$ right away, c.f. Line 3. That is, start or continue their operation at the requested power γ_a . Their operation will not be interrupted, and they remain must-run until the end of their operation.

Step 3: In Line 4, considering the list of appliances that have already become awake, update the probabilities at which other appliances will send an admission request in the upcoming time slots as in (22). Adopt (24) to update the probabilities with which sleeping devices become active in upcoming time slots, c.f. Line 5.

Step 4: Use the current information to calculate the expected load in the upcoming time slots using (25) as indicated in Line 6. Update the remaining required energy of each appliance at the beginning of the current time slot, i.e., E_t^a , using (1), c.f. Line 7.

Step 5: Next, set the "on" / "off" state of each awake controllable appliance for the rest of the time slots by solving optimization problem (18), c.f. Line 8.

Step 6: In Lines 9 to 11, if any non-interruptible controllable appliance became active (i.e., it switched from *off* to *on*) in Step 5, remove it from the list of controllable appliances and add it to list of must-run devices as it should remain on until it finishes its operation.

V. PERFORMANCE EVALUATION

In this section, we present simulation results and assess the performance of our proposed DSM algorithm. We run the simulation multiple times with different patterns for the times at which the appliances become awake. We then present the average results. Unless stated otherwise, the simulation setting is as follows. We assume that the general RTP method combined with IBR is adopted as described in (3). In our system model, the retail price parameters, m_t , n_t , and b_t , are set by the retail energy provider to compensate the cost of providing energy and to shape the daily energy consumption of the user. However, these parameters are different from the load cost profile of the energy provider, as the load cost

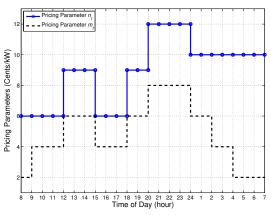


Fig. 3. The pricing parameters used based on the combined RTP and IBR pricing model in (3). Parameter $b_t = 3.5$ kW is fixed for all time slots.

profile of the energy provider is determined in the wholesale electricity market. The exact load cost profile of the retailer is usually not known to the end users. Fig. 3 illustrates the variation of parameters m_t and n_t of the price function over one day. We consider a single household with various mustrun and controllable appliances. Controllable appliances can be either interruptible or non-interruptible. Non-interruptible appliances include: electric stove ($E_a = 4.5$ kWh, $\gamma_a = 1.5$ kW), clothes dryer ($E_a = 1$ kWh, $\gamma_a = 0.5$ kW), and vacuum cleaner ($E_a = 3$ kWh, $\gamma_a = 1.5$ kW). Interruptible appliances include: Refrigerator ($E_a = 2.5$ kWh, $\gamma_a = 0.125$ kW), air conditioner ($E_a = 6$ kWh, $\gamma_a = 1.5$ kW), dishwasher ($E_a = 2$ kWh, $\gamma_a = 1$ kW), heater ($E_a = 4$ kWh, $\gamma_a = 1$ kW), water heater ($E_a = 2$ kWh, $\gamma_a = 1$ kW), pool pump ($E_a = 4$ kWh, $\gamma_a=2$ kW), and PEV ($E_a=10$ kWh, $\gamma_a=2.5$ kW). Mustrun appliances include: Lightning ($E_a = 3$ kWh, $\gamma_a = 0.5$ kW), TV ($E_a = 1$ kWh, $\gamma_a = 0.25$ kW), PC ($E_a = 1.5$ kWh, $\gamma_a = 0.25$ kW), ironing appliance ($E_a = 2$ kWh, $\gamma_a = 1$ kW), hairdryer ($E_a = 1$ kWh, $\gamma_a = 1$ kW), and others ($E_a = 6$ kWh, $\gamma_a = 1.5$ kW). The details of the average annual energy consumption of different appliances and the average monthly energy consumption of residential users in the US can be found in [35] and [36]. The time slot at which each appliance becomes awake is selected randomly from a pre-determined time interval, e.g. [6:00, 14:00] for electric stove and [16:00, 24:00] for PEV.

A. Performance Gains of Users and Utility Company

To have a baseline to compare with, we consider a system without ECC deployment, where each appliance a is assumed to start operation right after it becomes awake at its nominal power γ_a . As an upper bound, we also consider a system with ECC deployment in which all the demand information of the appliances is available ahead of time. Simulation results for the average total power consumption for the proposed residential load control algorithm, the system without ECC deployment, and the system in which complete demand information is available ahead of time are depicted in Fig. 4. In our simulation model, we set $b_t = 3.5$ kW in (3) for all time slots. As illustrated in Fig. 4, to reduce electricity payment, the ECC unit shifts the load to time slots with lower prices such as

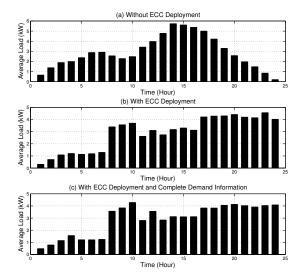


Fig. 4. Power consumption for (a) the system without ECC deployment, (b) the system with ECC deployment, and (c) the system with ECC deployment in which complete demand information is available ahead of time.

the after midnight hours. However, the high price penalty for exceeding the b_t threshold prevents *load synchronization* as discussed in Section II. The simulation results show that exploiting the use of the ECC unit reduces the average daily payment of the user from 4.76 Dollars/day to 4.01 Dollars/day. For the case, where complete information about the demand of each appliance is available ahead of time, the average daily payment of the user is 3.92 Dollars/day. To evaluate the PAR, the user's daily peak load is divided by his daily average load. That is, after running the algorithm, at the end of the operation period, we compute

$$PAR = \frac{T \max\{l_1, \dots, l_T\}}{\sum_{k=1}^{T} l_k},$$
(26)

where l_k is the total power consumption of the user at time slot k. The proposed algorithm also helps to reduce the average PAR of the system from 2.66 to 1.98 (25.5% PAR reduction) compared to the system without ECC deployment. The PAR of the system with ECC deployment if complete demand information is known a priori is 1.89.

B. Computational Complexity

In general, integer linear programs with n integer variables and m constraints are known to be NP-complete [37]. However, there exist pseudo-polynomial algorithms for solving $m \times$ n integer programs with fixed m which have an order of complexity of $O(n^{2m+2}(m\alpha)^{(m+1)(2m+1)}\log(n^2(m\alpha^2)^{2m+3}))$, where α is the maximum coefficient in the set of constraints [38]. A complete discussion of the complexity of such algorithms is out of the scope of this paper. To illustrate the complexity of our proposed algorithm, simulation results for the average run time of the algorithm, the number of integer variables, and the number of constraints for different numbers of appliances and different time granularities are given for one time slot in Table I. The order of complexity of the algorithm determines the maximum run-time or the maximum number of elementary operation required to solve the problem for

TABLE I Performance measures and complexity analysis of the proposed algorithm.

Time granularity	$ \mathcal{A} =20$	A =25	A =35
1 hour	0.0287	0.0308	0.0350
30 minutes	0.0294	0.0316	0.0422
15 minutes	0.0302	0.0318	0.0988

Average run time of the algorithm (in seconds).

Average number of integer variables.

-	-		
Time granularity	$ \mathcal{A} =20$	A =25	A = 35
1 hour	80	156	296
30 minutes	121	230	440
15 minutes	168	316	619

Average number of constraints.

Time granularity	$ \mathcal{A} =20$	<i>A</i> =25	A =35
1 hour	43	79	139
30 minutes	46	81	142
15 minutes	54	87	145

any input scenarios. In practice, the times at which different appliances become awake are distributed over the operation horizon, and it is unlikely that all appliances become awake at the same time. Thus, at each time slot, the number of awake appliances required to be scheduled is limited. This can significantly reduce the average run time of the algorithm in most practical scenarios. By increasing the time granularity, the number of integer variables and the number of constraints are increased, since the number of time slots at which the operation of each appliance should be scheduled is increased. However, the effect of this increase is mitigated, since the times at which different appliances become awake are distributed over a larger number of time slots, and the number of awake appliances in each time slot is reduced.

C. The Impact of Price Control Parameter b_t

Considering the price function as described in (3), in each time slot, if the power consumption of the user exceeds a certain threshold defined as b_t , the user will be penalized by paying a higher price. The choice of parameter b_t has a significant impact on users' payments and the PAR. To have a baseline to compare with, similar to [27], we consider a system in which the effect of IBR is ignored and only the basic price in each time slot is taken into account to schedule the operation of different appliances in order to minimize the electricity payment of the user. Simulation results for the average payment of the user and the PAR of the system for different values of parameter b_t are shown in Figs. 5 and 6, respectively. Intuitively, increasing the price parameter b_t for each time slot results in a reduction of the user's payment as shown in Fig. 5. Considering the average PAR, for the system without ECC deployment and the system without IBR consideration, the PAR does not change as the user does not respond to changes of parameter b_t . For the system with ECC deployment, for low values of parameter b_t , even the load of must-run appliances in most time slots exceeds this threshold. Thus, the ECC unit mainly considers the n_t price parameter to schedule the operation of controllable appliances.

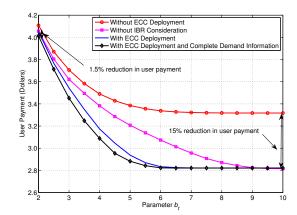


Fig. 5. The daily payment of the user for different values of parameter b_t .

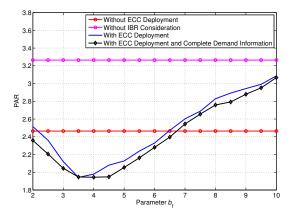


Fig. 6. PAR of the system for different values of parameter b_t .

However, by increasing parameter b_t , since the load of mustrun appliances lies below threshold b_t in some time slots, the user is encouraged to shift the controllable portion of its load to avoid paying higher price n_t rather than lower price m_t , which initially results in reducing the PAR. Later on, a further increase of parameter b_t reduces the effect of IBR, entails load synchronization effects, and increases the PAR of the system. That is, for large values of parameter b_t , it is less likely that the load of the user exceeds this threshold, and the ECC unit mainly pays attention to the value of the price parameter m_t in order to schedule the operation of controllable appliances. This results in shifting a large portion of the load to low price time slots. Therefore, for large values of parameter b_t , the performance of our proposed method approaches the one without IBR consideration as shown in Fig. 6.

D. The Impact of Adopting Inclining Block Rates

In this section, we examine how changes of the two parameters m_t and n_t of the price function will affect the performance of the system. In our simulation model, parameter m_t changes as illustrated in Fig. 3 and we set $b_t = 3$ kW for all time slots. However, parameter n_t is given by

$$n_t = \theta m_t, \quad \forall t \in \{1, \dots, T\}.$$
(27)

Simulation results for the average daily payment of the user as well as the average PAR of the system for different values of parameter θ are depicted in Figs. 7 and 8, respectively.

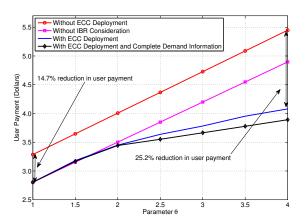


Fig. 7. The daily payment of the user for different values of parameter θ .

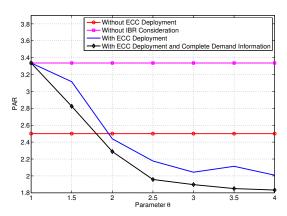


Fig. 8. PAR of the system for different values of parameter θ .

Intuitively, when θ is equal to one, i.e., when $m_t = n_t$ for all t, the performance of our proposed method is the same as the one in which the effect of IBR is ignored. However, by increasing parameter θ , the payment of the user will be increased, as the user has to pay more every time that its load exceeds threshold b_t as shown in Fig. 7. As indicated in Fig. 8, increasing parameter θ improves the PAR of the system, as load synchronization is prevented. That is, to avoid paying at higher price n_t , the ECC unit tries to distribute the load such that it does not exceed the b_t threshold. However, for the system without IBR consideration, changes of parameter θ do not affect the PAR.

VI. CONCLUSIONS

In this paper, we proposed an optimal residential load control algorithm for DSM in presence of load uncertainty. We formulated an optimization problem to minimize the electricity payment of the users in situations where only an estimate of the future demand is available. We focused on a scenario where real-time pricing is combined with IBRs to balance residential load to achieve a low PAR. Simulation results show that the proposed algorithm reduces the energy cost of users, encouraging them to participate in DSM. Exploiting IBR with RTP tariffs can help to avoid load synchronization, and the combination of the general RTP method with our algorithm reduces the PAR of the total load. The latter provides incentives for utilities to support implementing the proposed algorithm.

REFERENCES

- "IEEE guide for smart grid interoperability of energy technology and information technology operation with the electric power system (EPS), end-use applications, and loads," *IEEE Std 2030-2011*, pp. 1–126, Oct. 2011.
- [2] M. Fahrioglu and F. Alvarado, "Designing cost effective demand management contracts using game theory," in *Proc. of IEEE Power Eng. Soc. 1999 Winter Meeting*, New York, NY, Jan. 1999.
- [3] —, "Using utility information to calibrate customer demand management behavior models," *IEEE Trans. on Power Systems*, vol. 16, no. 2, pp. 317–322, May 2001.
- [4] R. Faranda, A. Pievatolo, and E. Tironi, "Load shedding: A new proposal," *IEEE Trans. on Power Systems*, vol. 22, no. 4, pp. 2086– 2093, Nov. 2007.
- [5] T. H. Yoo, H. G. Kwon, H. C. Lee, C. Rhee, Y. T. Yoon, and J. Park, "Development of reliability based demand response program in Korea," in *Proc. of IEEE Innovative Smart Grid Technologies*, Anaheim, CA, Jan. 2011.
- [6] A. Conejo, J. Morales, and L. Baringo, "Real-time demand response model," *IEEE Trans. on Smart Grid*, vol. 1, no. 3, pp. 236–242, Dec. 2010.
- [7] T. Jin and M. Mechehoul, "Ordering electricity via Internet and its potentials for smart grid systems," *IEEE Trans. on Smart Grid*, vol. 1, no. 3, pp. 302–310, Dec. 2010.
- [8] D. D. Weers and M. A. Shamsedin, "Testing a new direct load control power line communication system," *IEEE Trans. on Power Delivery*, vol. 2, no. 3, pp. 657–660, Jul. 1987.
- [9] A. Gomes, C. H. Antunes, and A. G. Martins, "A multiple objective approach to direct load control using an interactive evolutionary algorithm," *IEEE Trans. on Power Systems*, vol. 22, no. 3, pp. 1004–1011, Aug. 2007.
- [10] N. Ruiz, I. Cobelo, and J. Oyarzabal, "A direct load control model for virtual power plant management," *IEEE Trans. on Power Systems*, vol. 24, no. 2, pp. 959–966, May 2009.
- [11] A. H. Mohsenian-Rad, V. W. S. Wong, J. Jatskevich, R. Schober, and A. Leon-Garcia, "Autonomous demand-side management based on game-theoretic energy consumption scheduling for the future smart grid," *IEEE Trans. on Smart Grid*, vol. 1, no. 3, pp. 320–331, Dec. 2010.
- [12] P. Luh, Y. Ho, and R. Muralidharan, "Load adaptive pricing: An emerging tool for electric utilities," *IEEE Trans. on Automatic Control*, vol. 27, no. 2, pp. 320–329, Apr. 1982.
- [13] Y. Tang, H. Song, F. Hu, and Y. Zou, "Investigation on TOU pricing principles," in *Proc. of IEEE PES Transmission and Distribution Conf. Exhibition: Asia and Pacific*, Dalian, China, Aug. 2005.
- [14] M. Crew, C. Fernando, and P. Kleindorfer, "The theory of peak-load pricing: A survey," *Journal of Regulatory Economics*, vol. 8, no. 3, pp. 215–248, Nov. 1995.
- [15] S. Zeng, J. Li, and Y. Ren, "Research of time-of-use electricity pricing models in China: A survey," in *Proc. of IEEE Int'l. Conf. on Industrial Engineering and Engineering Management*, Singapore, Dec. 2008.
- [16] P. Samadi, A. H. Mohsenian-Rad, R. Schober, V. W. S. Wong, and J. Jatskevich, "Optimal real-time pricing algorithm based on utility maximization for smart grid," in *Proc. of IEEE Int'l. Conf. on Smart Grid Communications*, Gaithersburg, MD, Oct. 2010.
- [17] P. Samadi, A. H. Mohsenian-Rad, R. Schober, and V. W. S. Wong, "Advanced demand side management for the future smart grid using mechanism design," *IEEE Trans. on Smart Grid*, vol. 3, no. 3, pp. 1170– 1180, Sep. 2012.
- [18] A. H. Mohsenian-Rad and A. Leon-Garcia, "Optimal residential load control with price prediction in real-time electricity pricing environments," *IEEE Trans. on Smart Grid*, vol. 1, no. 2, pp. 120–133, Sep. 2010.
- [19] P. Samadi, R. Schober, and V. W. S. Wong, "Optimal energy consumption scheduling using mechanism design for the future smart grid," in *Proc. of IEEE Int'l. Conf. on Smart Grid Communications*, Brussels, Belgium, Oct. 2011.
- [20] N. Li, L. Chen, and S. H. Low, "Optimal demand response based on utility maximization in power networks," in *Proc. of IEEE Power and Energy Society General Meeting*, Detroit, MI, Jul. 2011.
- [21] P. Reiss and M. White, "Household electricity demand, revisited," *Review of Economic Studies*, vol. 72, no. 3, pp. 853–883, Jul. 2005.

- [22] S. Borenstein, "Equity effects of increasing-block electricity pricing," *Center for the Study of Energy Markets Working Paper*, vol. 180, Nov. 2008.
- [23] BC Hydro, *Electricity Rates*, 2009. [Online]. Available: http://www.bchydro.com/youraccount/content/electric_tariff.jsp
- [24] T. Hubert and S. Grijalva, "Realizing smart grid benefits requires energy optimization algorithms at residential level," in *Proc. of IEEE Innovative Smart Grid Technologies*, Anaheim, CA, Jan. 2011.
- [25] M. Pedrasa, T. Spooner, and I. MacGill, "Coordinated scheduling of residential distributed energy resources to optimize smart home energy services," *IEEE Trans. on Smart Grid*, vol. 1, no. 2, pp. 134–143, Sep. 2010.
- [26] R. Ferrero and S. Shahidehpour, "Short-term power purchases considering uncertain prices," *IEE Proceedings of Generation, Transmission and Distribution*, vol. 144, no. 5, pp. 423–428, Sep. 1997.
- [27] T. T. Kim and H. V. Poor, "Scheduling power consumption with price uncertainty," *IEEE Trans. on Smart Grid*, vol. 2, no. 3, pp. 519–527, Sep. 2011.
- [28] M. Parvania and M. Fotuhi-Firuzabad, "Demand response scheduling by stochastic SCUC," *IEEE Trans. on Smart Grid*, vol. 1, no. 1, pp. 89–98, Jun. 2010.
- [29] K. Cheung and R. Rios-Zalapa, "Smart dispatch for large grid operations with integrated renewable resources," in *Proc. of IEEE Innovative Smart Grid Technologies*, Anaheim, CA, Jan. 2011.
- [30] S. Tiptipakorn and W. Lee, "A residential consumer-centered load control strategy in real-time electricity pricing environment," in *Proc.* of North American Power Symposium, Las Cruces, NM, Oct. 2007.
- [31] G. Xiong, C. Chen, S. Kishore, and A. Yener, "Smart (in-home) power scheduling for demand response on the smart grid," in *Proc. of IEEE PES Innovative Smart Grid Technologies Conf.*, Anaheim, CA, Jan. 2011.
- [32] W. Powell, Approximate Dynamic Programming: Solving the Curses of Dimensionality. Wiley-Blackwell, 2007.
- [33] D. Bertsekas, Dynamic Programming and Optimal Control. Athena Scientific, Belmont, MA, 2005.
- [34] "MOSEK," 2012. [Online]. Available: http://www.mosek.com
- [35] U.S. Department of Energy, *The 2010 Buildings Energy Data Book*. Energy Efficiency and Renewable Energy, Mar. 2011.
- [36] "U.S. Energy Information Administration," 2012. [Online]. Available: http://www.eia.gov
- [37] C. Papadimitriou and K. Steiglitz, Combinatorial Optimization: Algorithms and Complexity. Dover Pubns, 1998.
- [38] C. Papadimitriou, "On the complexity of integer programming," J. of the ACM, vol. 28, no. 4, pp. 765–768, Oct. 1981.



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