

The exam is worth 40 pts (20% of course grade). Assuming 1 point per minute, try to finish in 40 minutes.

Use the following transform notations:

- $T(\mathbf{v})$ is translation by the vector \mathbf{v} .
- $S(s_x, s_y, s_z)$ is scaling by s_x in the x direction etc.
- $R_v(\theta)$ is rotation by θ around the vector \mathbf{v} .

1. Viewing (7pts)

- (5) Draw a picture of the pinhole camera model, clearly labeling the center of projection, view plane, focal length, field of view, and gaze direction.
- (2) Describe the location and view direction of the canonical pinhole camera in OpenGL.

2. Basic Transforms (5pts)

- (1) What is the inverse of the translation $T(\mathbf{v})$?
- (1) What is the inverse of the scaling transform $S(s_x, s_y, s_z)$?
- (1) What is the inverse of the rotation $R_x(\theta)$?
- (2) If $R_x(\theta)$ is represented as a matrix, what is the matrix equation for the inverse?

3. Using Transforms (10pts)

- (3) Assuming a combined model-view matrix \mathbf{VM} , what is \mathbf{V} for a camera at position \mathbf{p} rotated by θ around the axis \mathbf{v} from the canonical position.
- (3) Write the matrix equation for an *instance transform*.
- (4) Write the matrix equation for a rotation by \mathbf{R} around the point \mathbf{p} .

4. Geometry (6pts)

- (6) Describe two different techniques for reducing the complexity of geometry passing through a rendering pipeline without reducing apparent scene complexity?

5. Lighting (12pts)

- (4) What two shading components form the Lambertian shading model?
- (2) What component is added by the Phong shading model?
- (4) Given the four basic shading vectors (\mathbf{l} , \mathbf{n} , \mathbf{r} , and \mathbf{v}), what is the equation for the Lambertian shading model (without attenuation)?
- (4) What is the equation for the extra component added by Phong?