# On Distributed Space-Time Coding Techniques for Cooperative Wireless Networks and their Sensitivity to Frequency Offsets

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  - Performance of wireless systems often limited by fading due to multipath signal propagation.
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- Concept of multiple antennas may be transferred to cooperative wireless networks.
  - Multiple (single-antenna) nodes cooperate in order to perform a **joint transmission strategy**.



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- Concept of multiple antennas may be transferred to cooperative wireless networks.
  - Multiple (single-antenna) nodes cooperate in order to perform a **joint transmission strategy**.
- $\implies$  Nodes share their antennas by using a **distributed** STC scheme.



### **Examples for Cooperative Wireless Networks**

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Relay nodes may either be fixed stations or other mobile stations ('user cooperation diversity').

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#### ⇒ Distributed STC techniques suitable for both simulcast and relay-assisted networks.



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#### **Example:**

Space-time block codes (STBCs) from orthogonal designs (Tarokh et al. '99)



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- Focus on the Alamouti scheme (orthogonal STBC for N = 2 transmitters).



### Outline

#### ► Influence of the Frequency Offsets

- Conventional Alamouti Detection
- Zero-Forcing Detection and Maximum-Likelihood Detection
- Bit Error Probability
- Simulation Results
- Frequency-Offset Estimation
- Conclusions



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- Overall frequency offset for transmitted signal  $s_{\nu}(t)$ :
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- Quasi-static frequency-flat fading:
   Complex channel coefficients h<sub>1</sub>, ..., h<sub>N</sub>.
- $\implies$  Frequency offsets cause **time-varying phase**:

$$\overline{h}_{\nu}[k] \doteq h_{\nu} \cdot \mathrm{e}^{\mathrm{j} 2 \pi \zeta_{\nu} k}$$



### **Ideal Local Oscillators – Alamouti-Detection**

**Distributed Alamouti scheme** (N = 2 Tx nodes); **ideal** local oscillators (LOs),  $\zeta_1 = \zeta_2 = 0$ 

 $\implies \mathbf{y}[k] = \mathbf{H}_{eq} \mathbf{x}[k] + \mathbf{n}[k] \quad (1)$ 



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 $\mathbf{y}[k]$ : Received samples,  $\mathbf{x}[k]$ : Transmitted symbols,  $\mathbf{n}[k]$ : Noise samples,

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#### $\implies$ Alamouti detection:

$$\mathbf{z}[k] \doteq \mathbf{H}_{eq}^{\mathrm{H}} \mathbf{y}[k] = \mathbf{H}_{eq}^{\mathrm{H}} \mathbf{H}_{eq} \mathbf{x}[k] + \mathbf{H}_{eq}^{\mathrm{H}} \mathbf{n}[k]$$
$$= \left( |h_1|^2 + |h_2|^2 \right) \mathbf{x}[k] + \mathbf{H}_{eq}^{\mathrm{H}} \mathbf{n}[k] \quad (2)$$



### Non-Ideal Local Oscillators – Alamouti-Detection

**Channel matrix**  $\mathbf{H}_{eq}$  becomes

$$\overline{\mathbf{H}}_{eq}[k] = \begin{bmatrix} \overline{h}_1[k] & -\overline{h}_2[k] \\ \overline{h}_2^*[k+1] & \overline{h}_1^*[k+1] \end{bmatrix}. \quad (3)$$

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- (i) Frequency offsets **perfectly known** at the receiver  $\implies$  Receiver uses  $\overline{\mathbf{H}}_{eq}^{H}[k]$  for detection. Product matrix  $\overline{\mathbf{H}}_{eq}^{H}[k] \overline{\mathbf{H}}_{eq}[k]$  is close to diagonal matrix (for practical values of  $\zeta_1, \zeta_2$ ).



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- (ii) Non-perfect estimates  $\hat{\zeta}_{\nu} \doteq \zeta_{\nu} + \epsilon_{\nu}$  of the frequency offsets available at the receiver

 $\implies \text{Receiver uses} \quad \overline{\mathbf{H}}_{\mathrm{eq},\epsilon}^{\mathrm{H}}[k] = \begin{bmatrix} h_1^* \cdot \mathrm{e}^{-\mathrm{j}2\pi\hat{\zeta}_1 k} & h_2 \cdot \mathrm{e}^{\mathrm{j}2\pi\hat{\zeta}_2 (k+1)} \\ -h_2^* \cdot \mathrm{e}^{-\mathrm{j}2\pi\hat{\zeta}_2 k} & h_1 \cdot \mathrm{e}^{\mathrm{j}2\pi\hat{\zeta}_1 (k+1)} \end{bmatrix} \quad \text{for detection.}$ 

Depending on the quality of the estimates  $\hat{\zeta}_{\nu}$ , more or less severe **orthogonality loss**.



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- (a) **Zero-forcing** (ZF) detection: Use inverse matrix for detection instead of hermitian conjugate.
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- (a) **Zero-forcing** (ZF) detection: Use inverse matrix for detection instead of hermitian conjugate.
- (b) Maximum-likelihood (ML) detection.
  - **Performance** of ZF detection is virtually the same as that of ML detection in all cases.
  - Given ideal LOs Alamouti detection, ZF detection, and ML detection are equivalent.



- Non-ideal LOs, Alamouti detection or ZF detection
- Quasi-static frequency-flat fading
- ▶ QPSK symbols x[k] with **Gray mapping**  $[b_{1k}b_{2k}] \mapsto x[k]$ :
  - $[00] \mapsto \exp[j\pi/4] \qquad [01] \mapsto \exp[j3\pi/4]$  $[11] \mapsto \exp[j5\pi/4] \qquad [10] \mapsto \exp[j7\pi/4].$



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- $\blacktriangleright$  z[k] corresponding symbol after Alamouti detection/ ZF detection
- ▶ Let  $d_{\text{Re}}[k]$ ,  $d_{\text{Im}}[k]$  denote real and imaginary part of z[k] for high SNRs  $(E_s/N_0 \rightarrow \infty)$ ; may be determined **analytically**.



 $\implies$  BEP for bit  $b_{1k}$ :

$$P_{\mathrm{b1}}[k] = \mathrm{Q}\left(\sqrt{2 \frac{d_{\mathrm{Im}}^2[k]}{\left(|h_1|^2 + |h_2|^2\right)} \frac{E_s}{N_{\mathrm{O}}}}\right)$$

$$P_{\rm b1}[k] = 1 - Q\left(\sqrt{2 \frac{d_{
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if  $\operatorname{Im}\{x[k]\}$  and  $\operatorname{Im}\{z[k]\}$  have equal signs

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▶ Similarly for bit 
$$b_{2k}$$
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 $\implies$  **Overall average BEP** given blocks of  $L_{\rm B}$  QPSK symbols:

$$\bar{P}_{\rm b} = \frac{1}{2L_{\rm B}} \sum_{k=0}^{L_{\rm B}-1} \mathrm{E} \left\{ P_{\rm b1}[k] \right\} + \mathrm{E} \left\{ P_{\rm b2}[k] \right\}$$
(4)

else

(Expectation is with respect to the channel coefficients  $h_1$  and  $h_2$ .)



### Outline

Influence of the Frequency Offsets

#### **Simulation Results**

- Alamouti Detection and ZF/ ML detection
- Perfect and Non-Perfect Frequency-Offset Estimates
- Frequency-Offset Estimation
- Conclusions



- Uncoded transmission, Tx power normalized w.r.t. number of Tx nodes
- QPSK symbols, Gray mapping
- ▶ Quasi-static frequency-flat fading, Rice factor K = 0 dB
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- Alamouti detection (solid lines) vs.
   ZF/ ML detection (dashed lines)
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   Absolute errors of 2% ... 5%



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  - Training-Based Estimation Method
  - Blind Estimation Method
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### **Frequency-Offset Estimation**

#### **Training-Based Estimation Method**

- Estimating channel coefficients given known data symbols is dual to estimating data symbols given known channel coefficients => Principle of Alamouti detection can be applied.
- Average over the phase differences of several subsequent channel-coefficient estimates Explicit estimates for the frequency-offsets.



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#### **Blind Estimation Method**

- ▶ QPSK symbols: Raise the received samples to the power of four and perform an FFT  $\implies$  Spectral lines at  $4\zeta_1$  and  $4\zeta_2$  plus noise.
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**Frequency-offset estimation** in cooperating wireless networks is **more difficult** than in  $(1 \times 1)$ -systems.



## Conclusions

#### Influence of frequency offsets on the performance of a distributed Alamouti scheme

- Different receiver concepts (Alamouti detection, ZF detection, ML detection)
- Bit error probability given non-ideal local oscillators
- $\longrightarrow$  The performance of a distributed Alamouti scheme is very sensitive to frequency offsets.

#### **Frequency-offset estimates**

- Accurate frequency-offset estimates are required at the receiver (e.g. error of less than 3%)
- Two different methods for frequency-offset estimation
- $\longrightarrow$  Frequency-offset estimation is more difficult than in (1×1)-systems.

