Performance Analysis for a Fully Decentralized Transmit Power Allocation Scheme for Relay-Assisted Cognitive-Radio Systems

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Introduction

Cognitive-Radio (CR) Systems

- Utilize unused or partially occupied frequency bands in adaptive, unlicensed fashion ⇒ More efficient spectrum utilization
- Spectrum sensing and radio scene analysis ⇒ Dynamically adjust transmission parameters (carrier frequency, bandwidth, transmit power, ...)
- CR capabilities will be relevant, e.g., for ultra-wideband systems

Relay-Assisted CR Systems

- Focus on CR networks consisting of many low-power transceivers for short-range transmission (⇒ wireless sensor networks, personal area networks)
- ⇒ Relay assistance attractive to achieve connectivity and guarantee certain performance of CR systems
- Available relays: Inactive cognitive devices or dedicated cognitive relays
- So far only few papers on cognitive relaying techniques available

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Introduction

Novel aspects

- Frequency band chosen by CR relay network not completely unoccupied, but accommodates active primary (e.g., licensed) narrowband link
- Fully **decentralized** transmit power allocation (FD-TPA) scheme for CR relay network
- ⇒ **Goal:** Optimize performance of CR system while limiting interference level experienced by primary link



• System Model and Problem Formulation

- Transmission Protocol and Centralized Optimization Problem
- Fully Decentralized Transmit Power Allocation (FD-TPA) Scheme
- Performance Analysis
- Numerical Performance Results
- Conclusions

Basic Assumptions

- Short-range wideband or UWB CR system based on CDMA
- Source S and destination D assisted by N_r perfectly synchronized relays $R_1, ..., R_{N_r}$ using orthogonal spreading codes (spreading length N_{sp})
- \bullet Primary link $U_1 \! \rightarrow \! U_2$ active (e.g. WLAN link) in band of CR system
 - Small bandwidth ratio $ho:=B_{
 m U}/B_{
 m CR}\ll 1$
 - Relatively large transmit power P_{U_1} employed by primary transmitter U_1
 - Small maximum sum interference power ξ tolerated by primary receiver U_2
- Quasi-static scenario; block fading with channel impulse responses (CIRs)

$$\mathbf{h}_{X,Y} := [h_{X,Y}^{(0)}, \dots, h_{X,Y}^{(L_{X,Y})}]^{\mathrm{T}},$$

 $X, Y \in \{S, D, R_1, ..., R_{N_r}, U_1, U_2\}$

⇒ Corresponding CIR energies:

 $\alpha_{X,Y} := \sum_{l=0}^{L_{X,Y}} |h_{X,Y}^{(l)}|^2$

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 $\mathbf{X}, \mathbf{Y} \! \in \! \{\mathbf{S}, \mathbf{D}, \mathbf{R}_1, ..., \mathbf{R}_{N_{\mathrm{r}}}, \mathbf{U}_1, \mathbf{U}_2\}$

 \Rightarrow Corresponding CIR energies:

$$\alpha_{X,Y} := \sum_{l=0}^{L_{X,Y}} |h_{X,Y}^{(l)}|^2$$



Further Assumptions (require some network acquisition phase)

- D perfect knowledge of $\mathbf{h}_{\mathrm{S},\mathrm{D}}$ and $\mathbf{h}_{\mathrm{R}_i,\mathrm{D}}$ $(i=1,...,N_\mathrm{r})$
- R_i $(i = 1, ..., N_r)$ perfect knowledge of h_{S,R_i} and $h_{R_{i'},R_i}$ $(i' \neq i)$
- S and R_i $(i = 1, ..., N_r)$ aware of CIR energies α_{S,U_2} or α_{R_i,U_2} in direction of primary receiver U_2

Transmission protocol consists of two orthogonal time slots:

Time Slot I

- $\bullet~S$ broadcasts message to $R_1,...,R_{\mathit{N_r}}$ and D
- Transmit power $P_{\rm S}$ adjusted such that interference constraint is met:

 $\rho \, P_{\rm S} \, \alpha_{{\rm S},{\rm U}_2} \leq \xi$

Moreover, maximum power constraint $P_{
m S} \leq P_{
m S,max}$

• CR nodes $Y \in \{R_1, ..., R_{N_r}, D\}$ employ simple despreading for primary interference suppression and perform optimal MRC of received signal \Rightarrow

$$\gamma_{\mathrm{S}\to\mathrm{Y}} := \frac{P_{\mathrm{S}}\alpha_{\mathrm{S},\mathrm{Y}}}{\sigma_{\mathrm{i},\mathrm{Y}}^2 + \sigma_{\mathrm{n},\mathrm{Y}}^2}, \qquad \sigma_{\mathrm{i},\mathrm{Y}}^2 := \frac{P_{\mathrm{U}_1}\alpha_{\mathrm{U}_1,\mathrm{Y}}}{N_{\mathrm{sp}}}$$

• Relays receiving message with MRC output SINR $\gamma_{S \rightarrow R_i} \ge \gamma_{th}$ assumed to decode correctly (γ_{th} : threshold SINR)

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Transmission protocol consists of two orthogonal time slots:

Time Slot II

- If $\gamma_{S \rightarrow D} < \gamma_{target}$, D initiates relaying process by broadcasting beacon signal (γ_{target} : target SINR at destination)
- Those $N_{\rm r}' \leq N_{\rm r}$ relays R_i that have decoded successfully broadcast beacon signal to inform other relays and destination
- $\bullet\,$ Participating relays $R_{\it i}$ re-encode message and simultaneously retransmit it
- D performs optimal MRC of signals from S and R_i $(i = 1, ..., N'_r)$
- Transmit powers of participating relays R_i shall be chosen such that interference constraint and all power constraints are met
- MRC output SINR γ_D at destination shall be **maximized** to establish quick connection between S and D

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Optimization Problem

• Linear optimization problem:

$$\begin{array}{ll} \text{maximize} & \gamma_{\mathrm{D}} = \frac{1}{\sigma_{\mathrm{i},\mathrm{D}}^{2} + \sigma_{\mathrm{n},\mathrm{D}}^{2}} \sum_{i=1}^{N_{\mathrm{r}}'} P_{\mathrm{R}_{i}} \, \alpha_{\mathrm{R}_{i},\mathrm{D}} + \gamma_{\mathrm{S}\to\mathrm{D}} \\ \text{subject to} & \rho \sum_{i=1}^{N_{\mathrm{r}}'} P_{\mathrm{R}_{i}} \, \alpha_{\mathrm{R}_{i},\mathrm{U}_{2}} \leq \xi \\ & P_{\mathrm{R}_{i}} \leq P_{\mathrm{R}_{i},\mathrm{max}}, \qquad i = 1, ..., N_{\mathrm{r}}' \end{array}$$

• Parameters $\rho\!=\!B_{\rm U}/B_{\rm CR}$, ξ , and $P_{\rm R_{\it i},max}$ known throughout CR network

- Optimal solution can be found using linear programming techniques; requires central node C with knowledge of all CIR energies α_{R_i,D} and α_{R_i,U₂}
- Values α_{R_i,D}, α_{R_i,U₂} communicated to C; then C computes optimal transmit powers and feeds solution back to relays ⇒ Signaling overhead

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Decentralized Scheme

Fully Decentralized Transmit Power Allocation (FD-TPA) Scheme

- FD-TPA scheme maximizes MRC output SINR at destination node D according to best effort strategy
- Fully decentralized, i.e., performed solely by relays (no feedback from D)
- No exchange of channel information or transmit power values
- Based on beacon signals N'_r known throughout CR network
- Relay R_i $(i = 1, ..., N'_r)$ adjusts transmit power as

$$P_{\mathrm{R}_{i}} := \min\left\{P_{\mathrm{R}_{i},\mathrm{max}}, \frac{\xi}{\rho N_{\mathrm{r}}^{\prime} \alpha_{\mathrm{R}_{i},\mathrm{U}_{2}}}\right\}$$

⇒ Sum interference power at U_2 at most ξ , without any further interaction between relays

Moreover, $P_{\mathbf{R}_i} \leq P_{\mathbf{R}_i, \max}$ $(i = 1, ..., N_r')$ guaranteed

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Decentralized Scheme

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 \Rightarrow Sum interference power at U_2 at most $\xi,$ without any further interaction between relays

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 $(i=1,...,N_\mathrm{r}')$ guaranteed

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- System Model and Problem Formulation
- Performance Analysis
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- Desirable to have **analytical expressions** for assessing the **performance** of the FD-TPA scheme compared to non-cooperative transmission
- We derive expression for **CDF** of overall MRC output SINR γ_D at destination, treating CIR energies $\alpha_{X,Y}$ as **random** variables (Rayleigh fading)
- Analysis rather complicated as relaying is only performed if $\gamma_{S \to D} \,{<}\, \gamma_{target}$
- Final result requires **numerical evaluation** of certain integrals as closed-form solution does **not** seem **feasible**

Main steps in derivation

• Event $\mathcal{E}^{(\alpha)}$: Source accomplishes γ_{target} on its own $(\gamma_{S \to D} \geq \gamma_{\text{target}})$ \Rightarrow Conditional event probability $\Pr{\{\mathcal{E}^{(\alpha)} | P_S, \sigma_{i,D}^2\}}$ \Rightarrow Conditional CDF $C^{(\alpha)}(\gamma_D | P_S, \sigma_{i,D}^2)$

• Event $\mathcal{E}^{(\beta_{\kappa})}$: Source does not accomplish γ_{target} , set of active relays $I_r^{(\kappa)}$

- \Rightarrow Conditional event probability $\Pr\{\mathcal{E}^{(\beta_{\kappa})} | P_{S}\}$
- \Rightarrow Conditional CDF $C^{(\beta_{\kappa})}\left(\gamma_{\rm D}|P_{\rm S}, \sigma^2_{{\rm i},{\rm D}}, P_{{\rm R}_{i_1}}, ..., P_{{\rm R}_{i_N}}\right)$

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Main steps in derivation (cont'd)

- Source transmit power $P_{\rm S}$, relay transmit powers $P_{\rm R_{\it i}}$, and interference power $\sigma_{\rm i,D}^2$ at destination are random variables depending on $\alpha_{\rm S,U_2}$, $\alpha_{\rm R_{\it i},U_2}$, $\alpha_{\rm U_1,D}$
- Derive closed-form expressions for conditional event probabilities, conditional CDFs, and PDFs $p_1(P_{\rm S})$, $p_2(\sigma_{\rm i,D}^2)$, $p_3(P_{\rm R_i})$
- \Rightarrow Average CDF of $\gamma_{
 m D}$ can be calculated via numerical integration

$$\begin{split} \bar{C}(\gamma_{\mathrm{D}}) &= \int_{0}^{\infty} \int_{0}^{P_{\mathrm{S},\mathrm{max}}} \mathrm{Pr}\{\mathcal{E}^{(\alpha)} \mid P_{\mathrm{S}}, \sigma_{\mathrm{i},\mathrm{D}}^{2}\} \, C^{(\alpha)}\left(\gamma_{\mathrm{D}} \mid P_{\mathrm{S}}, \sigma_{\mathrm{i},\mathrm{D}}^{2}\right) p_{1}(P_{\mathrm{S}}) \, p_{2}(\sigma_{\mathrm{i},\mathrm{D}}^{2}) \\ &+ \left(1 - \mathrm{Pr}\{\mathcal{E}^{(\alpha)} \mid P_{\mathrm{S}}, \sigma_{\mathrm{i},\mathrm{D}}^{2}\}\right) \left(\sum_{\kappa=0}^{\psi-1} \int_{0}^{P_{\mathrm{R}_{i_{N_{\mathrm{r}}}}/\mathrm{max}}} \int_{0}^{P_{\mathrm{R}_{i_{1}},\mathrm{max}}} \mathrm{Pr}\{\mathcal{E}^{(\beta_{\kappa})} \mid P_{\mathrm{S}}\} \\ &\times C^{(\beta_{\kappa})}\left(\gamma_{\mathrm{D}} \mid P_{\mathrm{S}}, \sigma_{\mathrm{i},\mathrm{D}}^{2}, P_{\mathrm{R}_{i_{1}}}, \dots, P_{\mathrm{R}_{i_{N_{\mathrm{r}}}}}\right) p_{3}(P_{\mathrm{R}_{i_{1}}}) \cdots p_{3}(P_{\mathrm{R}_{i_{N_{\mathrm{r}}}}}) \\ &\times \mathrm{d}P_{\mathrm{R}_{i_{1}}} \cdots \mathrm{d}P_{\mathrm{R}_{i_{N_{\mathrm{r}}}}}\right) p_{1}(P_{\mathrm{S}}) \, p_{2}(\sigma_{\mathrm{i},\mathrm{D}}^{2}) \, \mathrm{d}P_{\mathrm{S}} \, \mathrm{d}\sigma_{\mathrm{i},\mathrm{D}}^{2} \end{split}$$

Main steps in derivation (cont'd)

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- \Rightarrow Average CDF of $\gamma_{\rm D}\,{\rm can}$ be calculated via numerical integration

$$\begin{split} \bar{C}(\gamma_{\rm D}) &= \int_{0}^{\infty} \int_{0}^{P_{\rm S,max}} \Pr\{\mathcal{E}^{(\alpha)} \mid P_{\rm S}, \sigma_{\rm i,D}^{2}\} \, C^{(\alpha)}(\gamma_{\rm D} \mid P_{\rm S}, \sigma_{\rm i,D}^{2}) \, p_{1}(P_{\rm S}) \, p_{2}(\sigma_{\rm i,D}^{2}) \\ &+ \left(1 - \Pr\{\mathcal{E}^{(\alpha)} \mid P_{\rm S}, \sigma_{\rm i,D}^{2}\}\right) \left(\sum_{\kappa=0}^{\psi-1} \int_{0}^{P_{\rm R_{i}}} \int_{0}^{P_{\rm R_{i}}} \Pr\{\mathcal{E}^{(\beta_{\kappa})} \mid P_{\rm S}\} \\ &\times C^{(\beta_{\kappa})}\left(\gamma_{\rm D} \mid P_{\rm S}, \sigma_{\rm i,D}^{2}, P_{\rm R_{i_{1}}}, ..., P_{\rm R_{i_{N_{r}}}}\right) p_{3}(P_{\rm R_{i_{1}}}) \cdots p_{3}(P_{\rm R_{i_{N_{r}'}}}) \\ &\times dP_{\rm R_{i_{1}}} \cdots dP_{\rm R_{i_{N_{r}'}}}\right) p_{1}(P_{\rm S}) \, p_{2}(\sigma_{\rm i,D}^{2}) \, dP_{\rm S} \, d\sigma_{\rm i,D}^{2} \end{split}$$

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- All link lengths normalized w.r.t. S–D link; S and D have fixed positions at (-0.5, 0) and (+0.5, 0); reference SNR $\bar{\gamma}_{0,S \rightarrow D}$
- $N_{\rm r} = 5$ relays R_i with positions (0,0), $(0,\pm 0.2)$, $(0,\pm 0.4)$ available
- Identical maximum transmit powers $P_{\max}=1$ for all CR nodes
- Threshold SINR at $R_i \ \gamma_{th} = 10 \text{ dB}$, target SINR at $D \ \gamma_{D,target} = 10 \text{ dB}$
- Primary transmitter U_1 /receiver U_2 located at (0, d+10) and (0, d)
- Average transmit power of U_1 $P_U = 10,000$; bandwidth ratio $\rho = 0.1$
- Maximum interference power tolerated by U_2 | $\xi = 0.01$

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- Average transmit power of U_1 $P_U = 10,000$; bandwidth ratio $\rho = 0.1$
- Maximum interference power tolerated by $U_2\ \ \xi\!=\!0.01$

Case 1:

SNR $\bar{\gamma}_{0,S\rightarrow D} = 5 \text{ dB}$

Spreading length $N_{\rm sp}\!=\!10$

Distance to primary users $d\!=\!3$

- - Non-cooperative transmission
- —– FD-TPA scheme

+ Simulation



FD-TPA scheme significantly outperforms non-cooperative transmission

Case 2:

 ${\rm SNR}\; \bar{\gamma}_{0,{\rm S}\rightarrow{\rm D}}\!=\!5\;{\rm dB}$

Spreading length $N_{\rm sp}\!=\!10$

Distance to primary users $d\!=\!12$

- - Non-cooperative transmission
- —– FD-TPA scheme
- x Simulation



Performance improves with growing distance d to primary users

Case 3:

 $\mathsf{SNR}\ \bar{\gamma}_{0,\mathrm{S}\rightarrow\mathrm{D}}\!=\!5\ \mathsf{dB}$

Spreading length $N_{\rm sp}\!=\!20$

Distance to primary users $d\!=\!12$

- - Non-cooperative transmission
- —– FD-TPA scheme
- o Simulation



Performance improves with growing spreading length $N_{ m sp}$

Case 4:

 $\mathsf{SNR}\ \bar{\gamma}_{0,\mathrm{S}\rightarrow\mathrm{D}}\!=\!10\ \mathsf{dB}$

Spreading length $N_{\rm sp}\!=\!10$

Distance to primary users $d\!=\!12$

- - Non-cooperative transmission
- —– FD-TPA scheme

* Simulation



Performance improves with growing SNR $\bar{\gamma}_{0,S \rightarrow D}$

Case 4:

 $\mathsf{SNR}\ \bar{\gamma}_{0,\mathrm{S}\rightarrow\mathrm{D}}\!=\!10\ \mathsf{dB}$

Spreading length $N_{\rm sp}\!=\!10$

Distance to primary users $d\!=\!12$

- - Non-cooperative transmission
- —– FD-TPA scheme
- * Simulation



Semi-analytical and simulation-based performance results in good accordance



Outage probability for FD-TPA scheme decreases significantly with growing distance d and is very close to optimal centralized (OC) solution



Outage probability for FD-TPA scheme decreases significantly with growing distance d and is very close to optimal centralized (OC) solution

- Fully decentralized transmit power allocation (FD-TPA) scheme for relay-assisted CR systems in the presence of active primary link
- FD-TPA scheme **maximizes SINR** at destination node of CR network while **limiting interference** experienced by primary receiver
- **Performance analysis** showed that FD-TPA scheme offers **significant improvements** over non-cooperative transmission and performs **closely** to optimal centralized solution
- Future work: Decentralized multi-hop solutions for further performance improvements (especially when primary system is very close by)