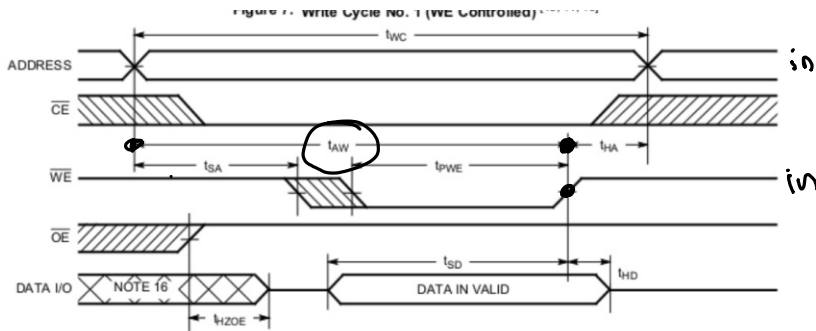
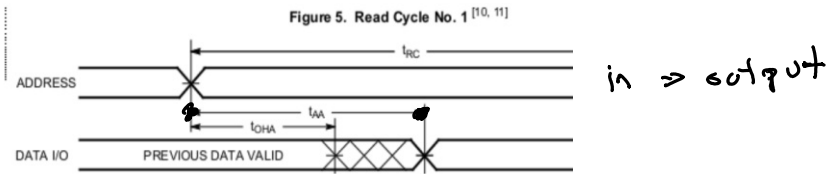


Memory System Design

Exercise 1: Is t_{AW} a requirement or a guaranteed specification for this memory? How about the t_{AA} ?



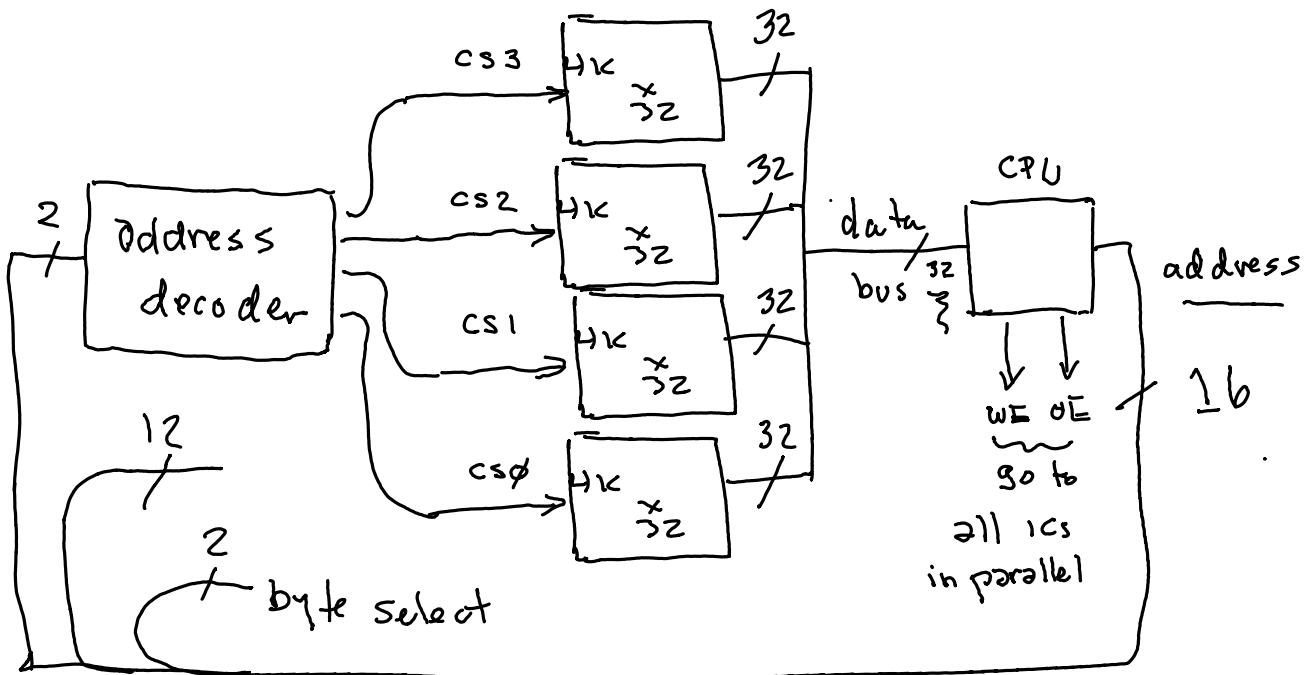
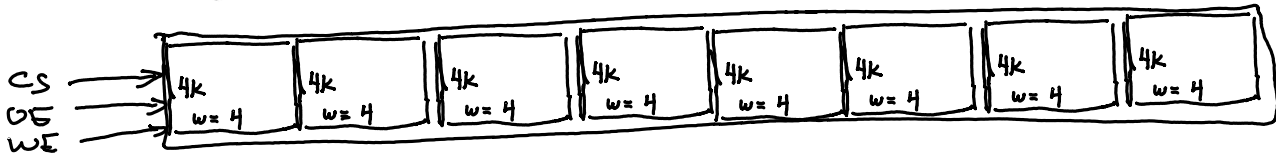
t_{AW} is requirement.



t_{AA} guaranteed specification.

Exercise 2: How many 4 kx4 memory IC's would be required to build a 16 k x 32 memory? What is the width of the data bus? How many address bus bits would be required? What address values could be placed on the address bus? How many chip-select lines would be required?

data bus
width = 32 bits



how many bits to address 16k x 32?
to select one of 16k words
requires... $2^n = 16k$

using calculator:

```
log2(16x1024)=
14.
```

$$16k = 16 \cdot 1024$$

$$16k = 2^4 \cdot 2^{10} = 2^{14}$$

$$\therefore n = 14$$

- $2^0 = 1$
- $2^1 = 2$
- 2 4 ←
- 3 8
- 4 16 ←
- 5 32
- 6 64
- 128
- 256
- 512
- 1024 ←

need 14 bits to select one of
16 k words

this is $16k \cdot \underbrace{\left(\frac{32}{8}\right)}_4$ bytes.

need additional 2 bits to select one of
4 bytes in a 32-bit word.

Our addresses have 16 bits (14 for word, 2 for byte)

$$0 \rightarrow 2^{16} - 1$$

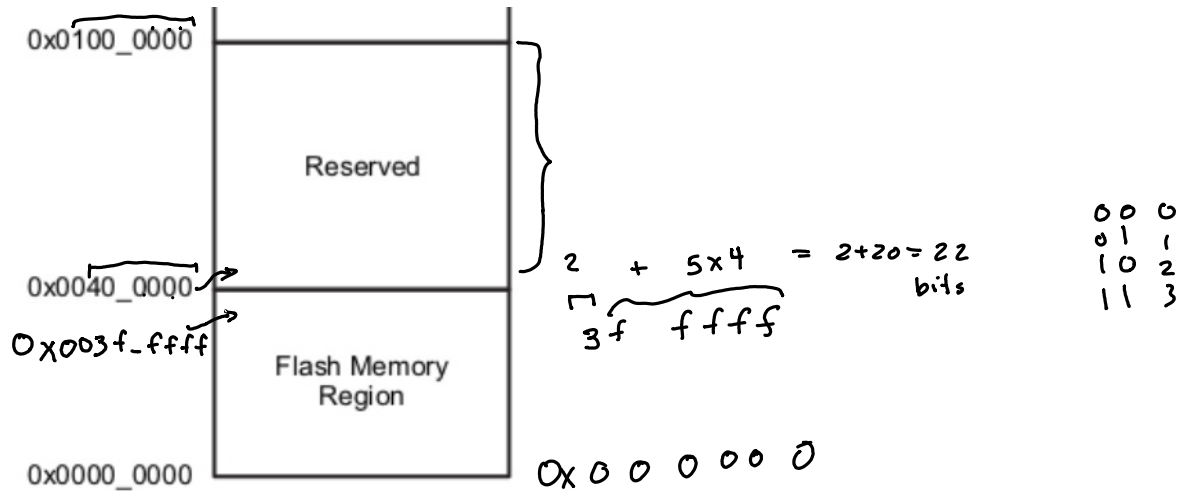
$$\underline{0} \rightarrow \underline{65535}$$

$$\text{to } \left(\begin{array}{c} 0 \dots 0 \\ 2^n - 1 \end{array} \right) \begin{array}{c} 0 \dots 0 \\ 1 \dots 1 \end{array}$$

$$\underline{0x0000} \rightarrow 0xffff$$

We have 4 banks so need 4 chip-selects.

Exercise 3: How large are the two lowest memory regions in the memory map above?



first region: #bytes = $2^n = 2^{22}$. ($0 \rightarrow 2^{22}-1$, $0x0 \rightarrow 0x3f_ffff$)

or subtract:

$$\begin{array}{r} 3f_ffff \\ - \quad \quad 0 \\ + \quad \quad \quad 1 \\ \hline \rightarrow 40_0000_{16} = \end{array}$$

```
ANS+DEC
4'194'304.
```

second region: $100\ 0000 \leftarrow$ address 1 past end

$$\begin{array}{r} 100\ 0000 \\ - 40\ 0000 \\ \hline c0\ 0000 \end{array} \leftarrow \text{start}$$

```
1000000-400000=
HEX c00000
```

$$\uparrow 10_{16} - 4_{16} = 16_{10} - 4_{10} = 12_{10} = c_{16}$$

or use calculator

Exercise 4: If a CPU has a 32-bit address bus, how many bytes can it address? What range of addresses would correspond to the first 64 k Bytes? If this range of memory was to be implemented with 32-bit words, how many address bits would be required to select a byte within each word? How many bits would be required to select a 32-bit word within the 64 k range? How many bits are not directly connected to the memory ICs? What are they be used for?

$$2^{30} \cdot 2^2 = 2^{10} \cdot 2^{10} \cdot 2^{10} \cdot 2^2$$

4 GB.

$$64 = 64 \cdot 1024$$

$$= 64 \cdot 1k$$

$$= 2^6 \cdot 2^{10}$$

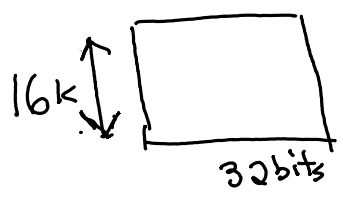
$$= 2^{16}$$

32 bits can address 2^{32} bytes.

first 64k bytes $\left\{ \begin{array}{l} 0 - (64k - 1) \quad 0 - 2^{16} - 1 \\ 0 - 0x10000 - 1 = 0 - 0xFFFF \end{array} \right.$

- 32 bit words = 4 byte words
so need 2 address bits as byte selects.

- 64 k bytes in 4-byte words



$$16k \times 4 \text{ bytes}$$

$$= 16k \times 32 \text{ bits.}$$

$$= 64 \text{ k bytes}$$

$$\text{is } \frac{64k}{4} = 16k \text{ words}$$

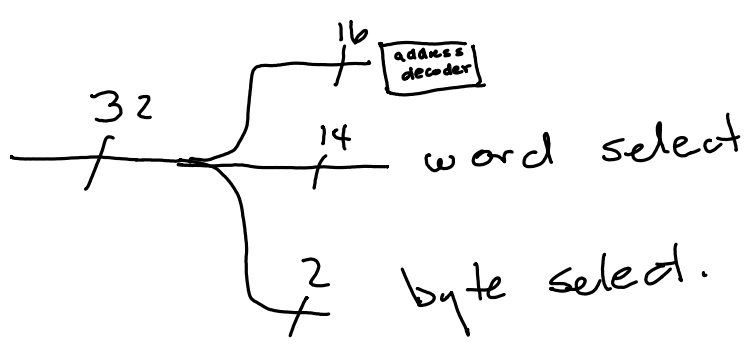
$$2^n = 16k \quad n = 14$$

need 14 bits to select a word.

$$16 \times 1024$$

$$2^4 \cdot 2^{10}$$

$$2^{14}$$

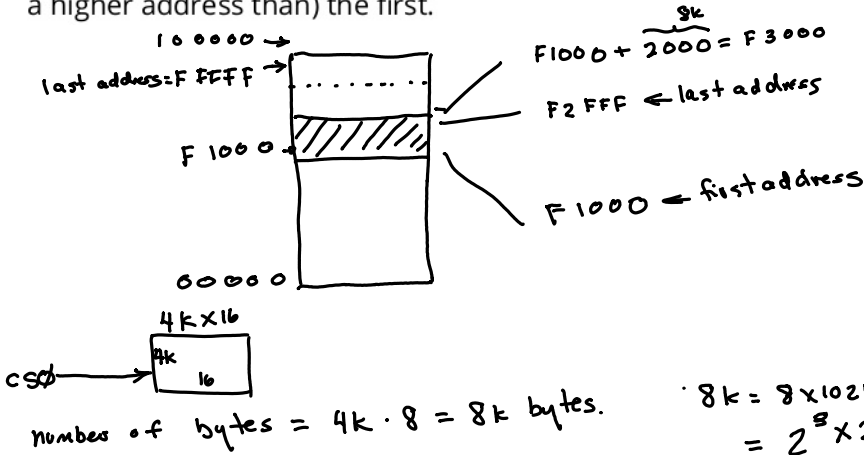


Exercise 5: A 4kx16 memory is to be used in a system with a 20-bit address bus. This memory is to respond to addresses starting at 0xf1000. Draw the memory map. Assuming the address signal is defined as signal A: std_logic_vector(19 downto 0); and the chip-select as signal CS0: std_logic; write the VHDL that would implement the chip-select signal CS0. Write the expression for CS1 if there was a second 4 kB bank immediately above (at a higher address than) the first.

$$0 - 2^{20} - 1$$

$$00000 \rightarrow FFFFF$$

$$F1000$$



$$8k = 8 \times 1024$$

$$= 2^3 \times 2^{10}$$

$$= 2^{13}$$

$$= 2000_{16} = 0x2000$$

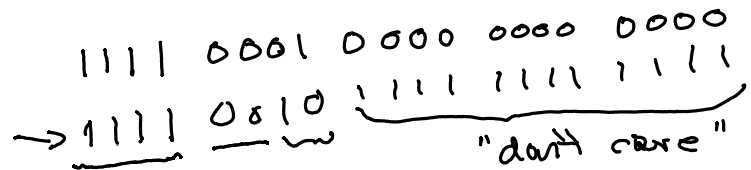
$$2^0 = 1$$

$$2^1 = 2$$

$$2^2 = 4$$

$$2^{13} = 8192$$

or $CS0 \leftarrow '1'$ when $A \geq x"F1000"$ and $A < x"F3000"$ else '0';
 $CS0 \leftarrow '1'$ when $A \geq x"F1000"$ and $A \leq x"F2FFF"$ else '0';



$CS0 \leftarrow '1'$ when $A(19 \text{ downto } 14) = "111100"$ and
 $(A(13 \text{ downto } 12) = "01"$ or
 $A(13 \text{ downto } 12) = "10")$ else '0';

$CS1 \leftarrow$